

DICE ACTIVITY Question: When rolling 2 dice what is the probability of getting a 2, 3, ... or 12?

- To understand this, here is a simulation and then define the theoretical probability.
- As we proceed through this activity, you will be introduced to basic probability rules and I have provided space for you to take notes.

Step 1: Simulation			Step 2: Defining a Probability Model		
Roll 2 dice and add them. Repeat 25 times. Here are the class results			List all the possible outcomes to get each sum. Use (dice1, dice2).		
2	2%	ESTIMATED Prob's	(1,1)	Sum of 2 Die	Probability
3	5%		(1,2) (2,1)	2	1/36 0.03
4	8%		(1,3) (2,2) (3,1)	3	2/36 0.06
5	10%		(1,4) (2,3) (3,2) (4,1)	4	3/36 0.08
6	15%		(1,5) (2,4) (3,3) (4,2) (5,1)	5	4/36 0.11
7	17%		(1,6) (2,5) (3,4) (4,3) (5,2) (6,1)	6	5/36 0.14
8	13%		(2,6) (3,5) (4,4) (5,3) (6,1)	7	6/36 0.16
9	12%		(3,6) (4,5) (5,4) (6,3)	8	5/36 0.14
10	10%		(4,6) (5,5) (6,4)	9	4/36 0.11
11	5%		(5,6) (6,5)	10	3/36 0.08
12	3%		(6,6)	11	2/36 0.06
TOTAL	100%			12	1/36 0.03

#possible outcomes = 36

$\Sigma = 36/36 \quad \Sigma = 1.00$

Theoretical Probability

DEFINITIONS:

- Sample Space (S):** The set of all possible outcomes of a chance process. **What is it here:**

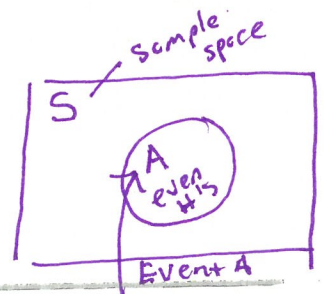
The list of all combinations of rolling 2 dice (circle and label)

- Probability Model:** A description of some chance process that consists of two parts: a sample space S and a probability for each outcome. **What is it here:**

- X is the list of all outcomes [label the column "X"]
- p(x) is the probability of each outcome [label the column "P(X)"]

Event

- An event is any collection of outcomes from some chance process.
- An event is a subset of the sample space.
- Events are designated by capital letters, like A, B, C, and so on



Find the following Probabilities (give as decimals, round to 2 decimals):

- 1) The probability of rolling a 5 is $P(5) = 0.11$
- 2) $P(6) = 0.14$ A probability must be between 0 and 1.
- 3) The probability of NOT rolling a 6 is $P(6^c) = 1 - 0.14 = 0.86$
- 4) $P(8^c) = 1 - 0.14 = 0.86$ This is the Complement rule.
- 5) $P(9) = 0.11$ $P(9^c) = 1 - 0.11 = 0.89$
- 6) Can you possibly roll both a 4 and a 5 at the same time? NO

ADD
"overlap"

- $P(4 \text{ and } 5) = 0$ $P(4 \cap 5) = 0$ \cap means Intersection (and)
- These events are Mutually exclusive; These are also called Disjoint events.

- 7) The probability of rolling a 2 or a 3 $P(2 \text{ or } 3) = P(2) + P(3) = 0.09$
- 8) $P(4 \text{ or } 5) = P(4) + P(5) = 0.19$ This is the Addition Rule rule.
For Mutually Exclusive Events
- 9) $P(6 \cup 7 \cup 8) = P(6) + P(7) + P(8) = 0.44$ U means Union (or)

OR
"Combine"

Basic Probability Rules (p301, p302, p304)

- 1) For any Event A: $0 \leq P(A) \leq 1$
- 2) If S is the sample space: $P(S) = 1$
- 3) Union of 2 events: $P(A \text{ or } B) = P(A \cup B)$
- 4) Intersection of 2 events: $P(A \text{ and } B) = P(A \cap B)$
- 5) Complement Rule: $P(A^c) = 1 - P(A)$
- 6) Mutually Exclusive (disjoint) Two events are mutually exclusive (disjoint) if they have no outcomes in common and so can never occur together.
- 7) Addition Rule for Mutually Exclusive Events: $P(A \text{ or } B) = P(A \cup B) = P(A) + P(B)$
- 8) General Addition Rule: $P(A \text{ or } B) = P(A \cup B) = P(A) + P(B) - P(A \text{ and } B)$

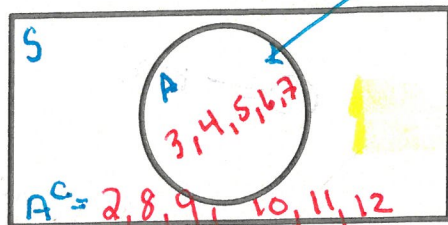
USING VENN DIAGRAMS: They are very helpful to understand probabilities.

Let:

- Event A: rolling 2 dice with sums 3-7
- Event B: rolling 2 dice with sums 7-10

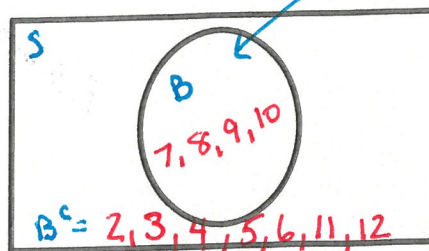
Draw Venn diagrams to find these probabilities:

$$P(A) = 0.55$$



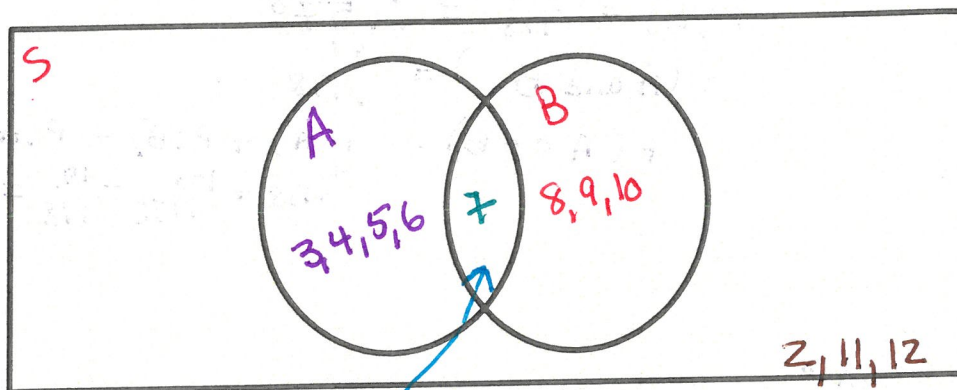
$$P(A^c) = 1 - P(A) = 0.45$$

$$P(B) = 0.49$$



$$P(B^c) = 1 - P(B) = 0.51$$

Draw the Venn Diagram to combine Events A and B and then answer these questions. Fill in the probability syntax:

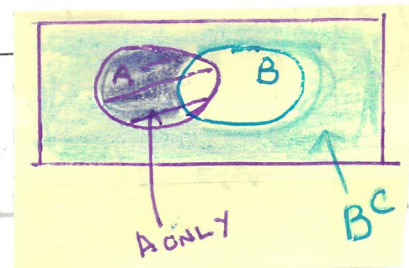
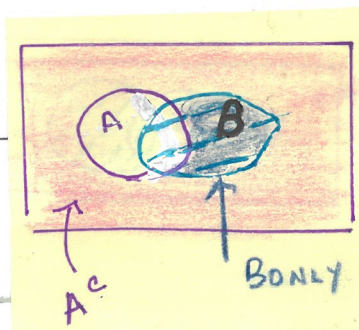


$$1. P(A \text{ and } B) = P(A \cap B) = P(7) = 0.16 \quad [\text{INTERSECT}]$$

$$2. P(A \text{ or } B) = P(A \cup B) = \frac{P(A) + P(B) - P(A \text{ and } B)}{0.55 + 0.49 - 0.16} = 0.88 \quad [\text{UNION}]$$

$$3. P(\text{ONLY } A) = P(A \text{ and } B^c) = \frac{P(3) + P(4) + P(5) + P(6)}{P(A) - P(A \text{ and } B)} = 0.39$$

$$4. P(\text{ONLY } B) = P(A^c \text{ and } B) = \frac{P(8) + P(9) + P(10)}{P(B) - P(A \text{ and } B)} = 0.33$$



EXAMPLE

Who Has Pierced Ears?

Two-way tables and probability



Students in a college statistics class wanted to find out how common it is for young adults to have their ears pierced. They recorded data on two variables—gender and whether the student had a pierced ear—for all 178 people in the class. The two-way table below displays the data.

Gender	Pierced Ears?		Total
	Yes	No	
Male	19	71	90
Female	84	4	88
Total	103	75	178

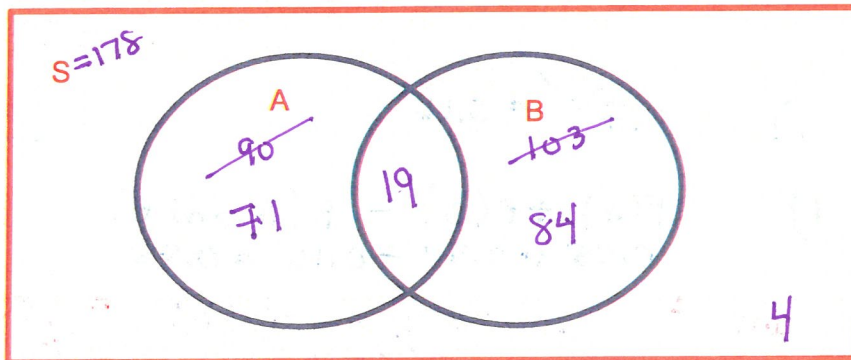
Handwritten notes on the table:
 $P(A \text{ and } B)$ points to the 19 in the Male/Yes cell.
 $P(A)$ points to the 90 in the Male Total cell.
 $P(B)$ points to the 103 in the Total/Yes cell.
 A red arrow points from the 4 in the Female/No cell to the text "# GO IN Venn diagram".

Let:
A=Males
B=Pierced Ears

Suppose we choose a student at random. Find the probability that the student (use correct probability notation, give as a fraction, and decimal)

- Has pierced ears. $P(B) = \frac{103}{178} = 0.579$
- Is male with pierced ears. $P(A \text{ and } B) = \frac{19}{178}$
- Is male or has pierced ears. $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$
 $\frac{90}{178} + \frac{103}{178} - \frac{19}{178} = \frac{174}{178} = 0.978$

Fill in the Venn Diagram to combine Events A and B and then answer these questions. (use correct probability notation and give as a fraction ONLY)



- $P(\text{male and pierced ears}) = P(A \text{ and } B) = \frac{19}{178} = 0.107$
- $P(\text{female and pierced ears}) = P(A^c \text{ and } B) = \frac{84}{178} = 0.472$
- $P(\text{female and no pierced ears}) = P(A^c \text{ and } B^c) = \frac{4}{178} = 0.022$

ASK YOUR SELF: DO YOU FIND PROBABILITY USING A TABLE OR VENN DIAGRAM?