

**KEY**

# Chapter 1 Study Guide: Exploring Data

WITH T184 PWS

**ACTIVITY 1.2**

**Individuals:** The objects described by a set of data. (ex: people, animals, things...)

**Variable:** Any characteristic of an individual.

**Categorical Variable:** Places an individual into groups or categories. (ex: colors)

**Quantitative Variable:** Variables that are numbers. (ex: height, weight)

Includes  
TPS 1.53+  
1.105


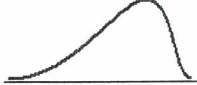
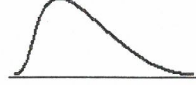
**Describe Distribution:**

- Shape: symmetric or skewed
  - Outliers: value that is outside pattern
  - Center: mean/median
  - Spread(Variability): range
- } + CONTEXT



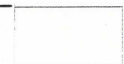
**Compare Distributions:**

Use comparative words (similar, greater than, less than)

**SHAPE of a distribution:** Use -ly words (slightly, moderately, strongly)

Symmetric	Skewed Left	Skewed Right
		
Mean = Median	Mean < Median	Mean > Median

Other words to describe shape:

Unimodal	Bimodal	Uniform
		

**CENTER of a distribution:**

- ~Mean:  $\longrightarrow$  Use with symmetric data
- ~Median: middle point of a distribution ( $location = \frac{n+1}{2}$ )  $\longrightarrow$  Use with skewed data

**SPREAD/VARIABILITY of a distribution:**

- ~Range = max - min
- ~Standard Deviation =  $\sqrt{variance}$   $\longrightarrow$  The average distance from the mean
- $\longleftarrow$  The (context) typically varies by (SD) from the mean by ( $\bar{x}$ ).
- ~IQR =  $Q_3 - Q_1$

**Resistant:** A measure that is unaffected by extreme values (ex-median)

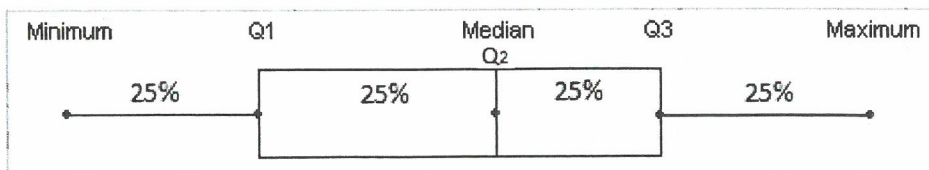
- ~Skewed data or outliers  $\rightarrow$  Use median and IQR
- ~Symmetric data  $\rightarrow$  Use mean and standard deviation

**OUTLIERS:**  
LFence:  $Q_2 - 1.5(IQR)$   
UFence:  $Q_3 + 1.5(IQR)$

**5 Number Summary:** MIN  $Q_1$  MED  $Q_3$  MAX  $\longrightarrow$  Use to make boxplot

**Outliers:** way too small  $< Q_1 - 1.5IQR$  and way too big  $> Q_3 + 1.5IQR$

**Boxplots:**



53. **Traveling to work** How long do people travel each day to get to work? The following table gives the average travel times to work (in minutes) for workers in each state and the District of Columbia who are at least 16 years old and don't work at home.<sup>30</sup>

AL	23.6	LA	25.1	OH	22.1
AK	17.7	ME	22.3	OK	20.0
AZ	25.0	MD	30.6	OR	21.8
AR	20.7	MA	26.6	PA	25.0
CA	26.8	MI	23.4	RI	22.3
CO	23.9	MN	22.0	SC	22.9
CT	24.1	MS	24.0	SD	15.9
DE	23.6	MO	22.9	TN	23.5
FL	25.9	MT	17.6	TX	24.6
GA	27.3	NE	17.7	UT	20.8
HI	25.5	NV	24.2	VT	21.2
ID	20.1	NH	24.6	VA	26.9
IL	27.9	NJ	29.1	WA	25.2
IN	22.3	NM	20.9	WV	25.6
IA	18.2	NY	30.9	WI	20.8
KS	18.5	NC	23.4	WY	17.9
KY	22.4	ND	15.5	DC	29.2

(a) Make a histogram of the travel times using classes of width 2 minutes, starting at 14 minutes. That is, the first class is 14 to 16 minutes, the second is 16 to 18 minutes, and so on.

(b) The shape of the distribution is a bit irregular. Is it closer to symmetric or skewed? About where is the center of the data? What is the spread in terms of the smallest and largest values? Are there any outliers?

PART A - Complete and add a boxplot

PART B - Complete and answer w/ Cuss and BS

## STUDY TIP FOR CH 1 TEST

TPS 1.53 - See my website for notes on CALC COMMANDS

Goal: become familiar with calculator.

STEP 1: FIND THE MEAN, STANDARD DEVIATION AND SAMPLE SIZE AND USE THE CORRECT VARIABLE NOTATIONS

STEP 2: FIND THE 5 NUMBER SUMMARY

STEP 3: CALC. IF THEIR ANY OUTLIERS

STEP 4: BASED ON THE MEAN AND MEDIAN WHAT DO YOU THINK THE SHAPE WILL BE?



**ANSWER KEY TO GIVEN QUESTIONS**

CH 1 STUDY TIP TIPS 1.53

53. **Traveling to work** How long do people travel each day to get to work? The following table gives the average travel times to work (in minutes) for workers in each state and the District of Columbia who are at least 16 years old and don't work at home.<sup>30</sup>

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**KEY** X = STATE AVG. TRAVEL TIME TO WORK (MIN)

STEP 1: Sample Mean =  $\bar{x} = 23.1$

Sample S.D =  $s_x = 3.6$

Sample size =  $n = 51$

STEP 2:

MIN = 15.5

Q1 = 20.8

MED = 23.4

Q3 = 25.2

MAX = 30.9

IQR = 4.4

R = 15.4

STEP 3:

IQR =  $25.2 - 20.8 = 4.4$

UB:  $1.5 * 4.4 + 25.2 = 31.8^+$

LB:  $20.8 - 1.5 * 4.4 = 14.2^-$

NO OUTLIERS MAX = 30.9 < 31.8

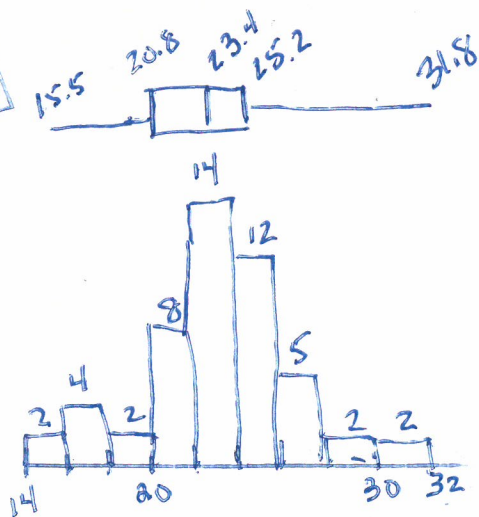
MIN = 15.5 > 14.2

STEP 4: Since the mean (23.1) and median (23.4) are close, I am expecting a somewhat symmetric shape.

(a) Make a histogram of the travel times using classes of width 2 minutes, starting at 14 minutes. That is, the first class is 14 to 16 minutes, the second is 16 to 18 minutes, and so on.

(b) The shape of the distribution is a bit irregular. Is it closer to symmetric or skewed? About where is the center of the data? What is the spread in terms of the smallest and largest values? Are there any outliers?

**Part A**



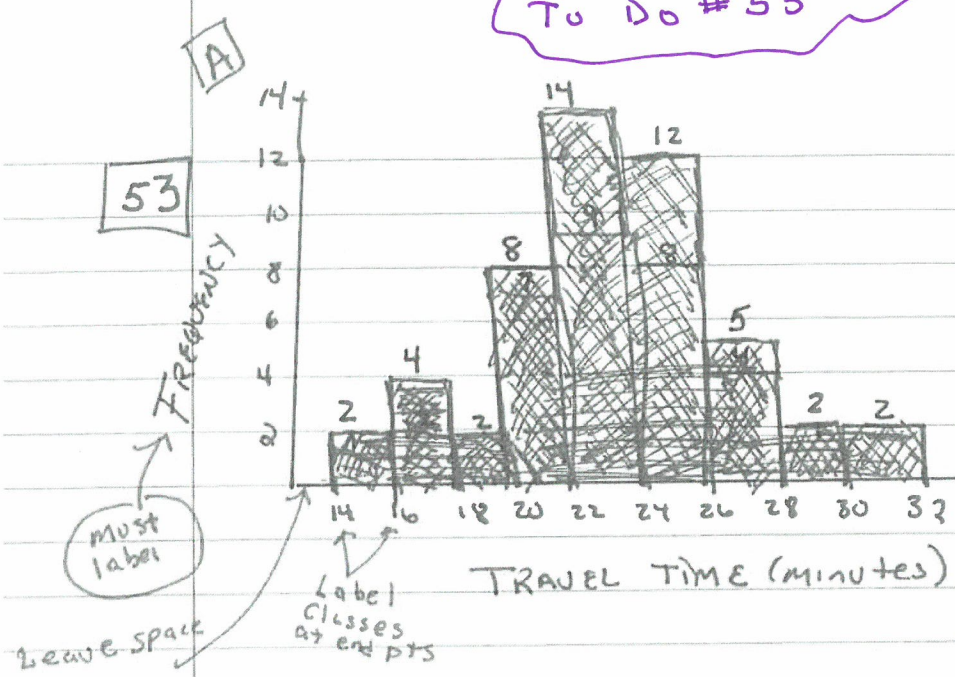
Need to label + include UNITS on ALL GRAPHS

**PART B**

FOR THE DISTRIBUTION OF TIME TRAVELED TO WORK, THE STATE DATA IS ROUGHLY SYMMETRIC. THE CENTER TRAVEL TIME IS ABOUT 23 MINUTES TO WORK WITH A SPREAD OF ABOUT 3.6 MINUTES. THERE APPEARS TO BE NO OUTLIERS

**CALC COMMANDS  
TO DO #53**

NOTE: GRAPHS DO NOT NEED TO BE ARTIST MASTER PIECES. IN STATS, WE GRAPH TO GET A VISUAL UNDERSTANDING OF THE DATA. LABELS ARE IMPORTANT.



Must label ← Give units

Make sure to get to know your calculator. You can use it on all tests. It's a GREAT tool.

- STEPS:
- Put the data in a LIST **STAT** EDIT L1
  - Zoom** **STAT:9** to see the graph
  - Set the **Window** to easily graph
 

The problem ask you to setup like this	}	$X_{MIN} = 14$	$Y_{MIN} = 0$	] these may vary
		$X_{MAX} = 32$	$Y_{MAX} = 14$	
		$X_{SCL} = 2$	$Y_{SCL} = 2$	
  - USE **TRACE** TO GET FREQUENCY COUNTS FOR EACH BAR (YOU DO NOT NEED TO INCLUDE THESE ON YOUR GRAPH, BUT THEY CAN BE HELPFUL INTERPRETING YOUR DATA.)
  - GET STATISTICS **STAT** **CALC** 1:1-VAR STATS **LI**  
 $\bar{X} = 23.1$   $S_x = 3.57$   $n = 51$   $MIN = 15.5$   $MED = 23.4$   $MAX = 30.9$

**B** ALTHOUGH THE GRAPH IS SOMEWHAT IRREGULAR, THE DISTRIBUTION IS ROUGHLY SYMMETRIC. FROM THE GRAPH THE CENTER IS ABOUT 23 MIN. THE SPREAD MEASURED BY THE RANGE IS ABOUT 15 MIN. THERE DO NOT APPEAR TO BE ANY OUTLIERS.



# KEY

105. SSHA scores Here are the scores on the Survey of Study Habits and Attitudes (SSHA) for 18 first-year college women:

pg 66



154	109	137	115	152	140	154	178	101
103	126	126	137	165	165	129	200	148

and for 20 first-year college men:

108	140	114	91	180	115	126
92	169	146	109	132	75	88
113	151	70	115	187	104	

Do these data support the belief that women have better study habits and attitudes toward learning than men? (Note that high scores indicate good study habits and attitudes toward learning.) Follow the four-step process.\*

THE 4 STEP PROCESS IS A GUIDE TO HELP YOU AND YOU DO NOT NEED TO DO THE STEPS EXACTLY.

## STEPS:

① (STATE) read question clearly and understand what you ARE ASKED TO ANALYZE. (mental step). What are you asked to ANALYZE? \_\_\_\_\_

② (PLAN/DO) What graphs + statistics do you need to support your claim?

Ⓐ STATISTICS: To provide include sample size ( $n$ ), mean ( $\bar{x}$ ), st dev ( $s_x$ ) and the 5 number summary

Ⓑ HISTOGRAMS: To see shape of distributions

Ⓒ BOX PLOTS: To identify outliers or do the calc's

$$LF = Q1 - 1.5 IQR$$
$$UF = Q3 + 1.5 IQR$$

Show work on BACK →

③ (CONCLUDE) ANSWER QUESTION IN CONTEXT.

# #105 KEY

① (STATE) The question is "Does the data for first year college students indicate women have better study habits and attitudes towards learning"

② (PLAN/DO) A

## Sample statistics

→ [L1] women SSHA  
→ [L2] men SSHA

GROUP	n	$\bar{x}$	$S_x$	MIN	Q <sub>1</sub>	Med	Q <sub>3</sub>	MAX
Women	18	114	26	101	126	139	154	200
men	20	121	33	70	98	115	143	187

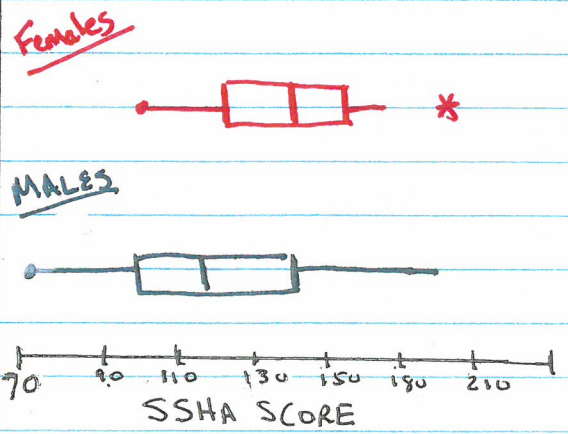
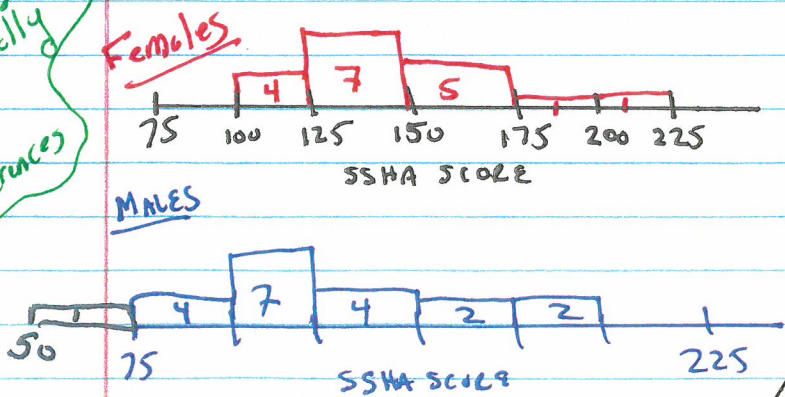
CALC - since sample sizes are different USE: 1-VAR STATS

③ HISTOGRAMS (STACK THEM TO SEE DIFFERENCES AND USE SAME SCALE) AND SHAPE OF DISTRIBUTIONS)

④ Box PLOTS (stack them + make sure to label and show scale, ALSO identify outliers)

Graphs do NOT need to be precise but show differences visually

### SSHA SCORE

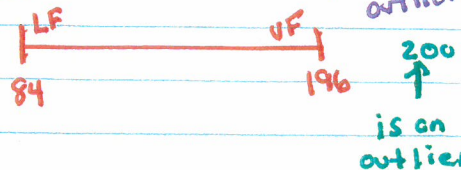


NOTE: TIGHT BOX PLOTS INDICATE OUTLIERS WITH A \*

OTHERWISE YOU NEED TO CALC:

Females  $IQR = 154 - 126 = 28$   
 $LF: 126 - 1.5(28) = 84$  (NO OUTLIER)  
 $UF: 154 + 1.5(28) = 196$  (OUTLIER = 200)

Visually



ANY DATA OUTSIDE THE FENCES ARE OUTLIERS



#105

### ③ CONCLUDE:

#### GUIDELINES FOR COMPARISONS:

You must compare Males and Females  
Shape, Center, Spread, outliers  
IN CONTEXT.

From the statistics and graphs, you can see 1<sup>st</sup> year female college students have higher SSHA (STUDY HABITS AND ATTITUDE) score than MALES.

- ① The <sup>Female</sup> center is higher than males for SSHA (based on mean, median, box plots)
- ② The Female SSHA spread is smaller than for males (based on SD, histograms, box plots) indicating there is less variability among Female SSHA scores.
- ③ Both Females and Males appear to have symmetric shape (based on histograms)