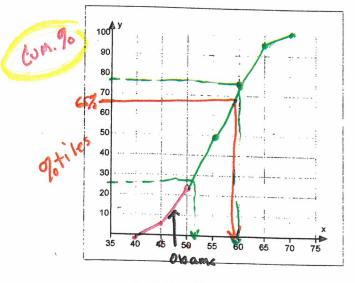
## 2.1A Activity

# Cumulative Relative Frequency

Example 1) President's Age at Inauguration

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|-------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------|-------------------------------|
| Age   | Frequency                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Relative frequency                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | Cumulative frequency | Cumulative relative frequency |
| 40-44 | 2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 2/44 = 0.045, or 4.5%                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 2                    | 2/44 = 0.045, or 4.5%         |
| 45-49 | 7                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 7/44 = 0.159, or $15.9%$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 9                    | 9/44 = 0.205, or 20.5%        |
| 50-54 | 13                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 13/44 = 0.295, or $29.5%$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 22                   | 22/44 = 0.500, or 50.0%       |
| 55-59 | 12                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 12/44 = 0.273, or $27.3%$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 34                   | 34/44 = 0.773, or 77.3%       |
| 60-64 | 7                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 7/44 = 0.159, or $15.9%$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 41                   | 41/44 = 0.932, or 93.2%       |
| 65-69 | 3                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 3/44 = 0.068, or 6.8%                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 44                   | 44/44 = 1.000, or 100%        |

1) Use the above cumulative relative frequency table to create a cumulative relative frequency graph.



- 2) USE THE GRAPH TO ANSWER THESE QUESTIONS AND ANSWER IN CONTEXT:
- A) What percent of Presidents were between 55 and 60 when they were inaugurated? 27.3%
- B) Was President Obama, who was inaugurated at 47 unusually young?

C) Estimate and interpret the 65 percentile of the distribution

About 65% of Us Presidents were younger than 57 (58).

D) Estimate the IQR?

IQL = 60-51 = (9)

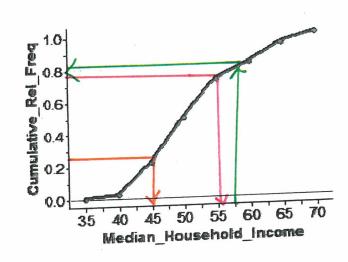
AGE AT IN AUGUR ATTON

\* 45 GOES WITH 45-50 AGE GROUP



# **Example 2: State Median Household Incomes**

Here is a cumulative relative frequency graph showing the distribution of median household incomes for the 50 states and the District of Columbia. Answer the following question (in context):



a) California, with a median household income of \$57,445 is at what percentile?

Coliforinia's median HH percentle b) What is the 25<sup>th</sup> percentile for this distribution? What is another name for this value?

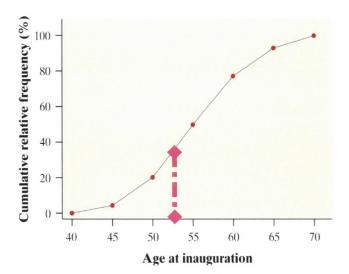
Q1-25th 2 tide is about \$46,000

c) Estimate the IQR

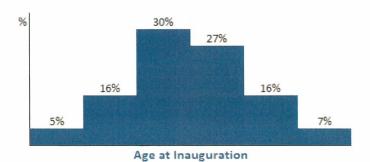
d) Where is the graph the steepest? What does this indicate about the distribution?

#### cumulative relative frequency graph,

[1] plot a point corresponding to the cumulative relative frequency in each class at the smallest value of the next class.

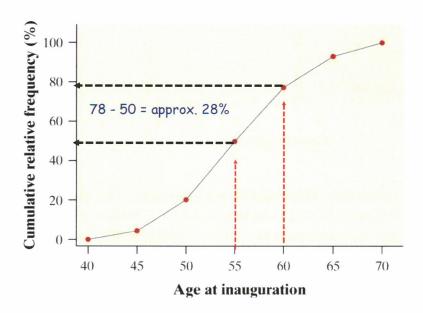


Describe the distribution: Hint sketch a histogram. The steeper the graph the larger the percentage of the data in that category. Notice, the graph is steepest between 50-55 and that accounts for 30% of the presidents ages.



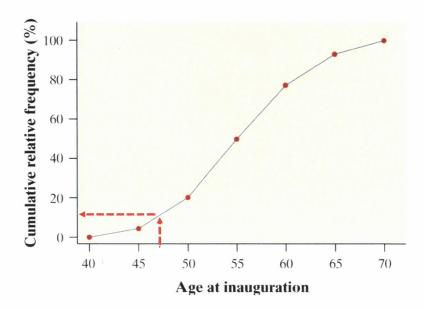
# 2A) What percent of Presidents were between 55 and 60 when they were inaugurated?

 $\bullet$  <u>ABOUT</u> 28% of all U.S. Presidents were between 55 and 60 years old at inauguration.

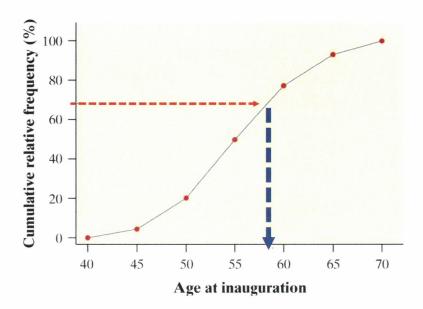


2B) Was President Obama, who was inaugurated at 47, unusually young?

• <u>ABOUT</u> 11% percent of all U.S. Presidents were younger than 47 years o at inauguration. Obama was unusually younger. He was younger than 89% of all U.S. Presidents.

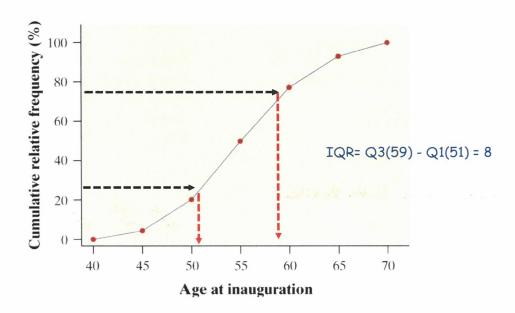


- 2C) Estimate and interpret the 65 percentile of the distribution.
- About 65% of U.S. Presidents were younger than 58 at the time of their inauguration.

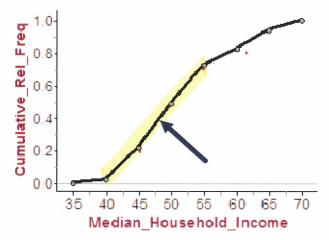


# 2D) Estimate IQR

• The middle 50%, the IQR, of all U.S. Presidents age at the time of their inauguration was about 8 years.



**Example 2: State Median Household Incomes** Here is a cumulative relative frequency graph showing the distribution of median household incomes for the 50 states and the District of Columbia. Answer the following question (in context):



- a) California, with a median household income of \$57,445 is at what percentile?
- California's median HH income is at the 78th percentile.

- b) What is the 25<sup>th</sup> percentile for this distribution? What is another name for this value?
- The 25th percentile for median HH income is about \$46,000. This is also called Quartile 1.

#### c) Estimate the IQR

- IQR = Q3 = \$55,000 Q1 = \$46,000 = \$9,000
- The middle 50% of HH Income by state is about \$9,000.
  - d) Where is the graph the steepest? Between 45-50

What does this indicate about the distribution? This is the largest % of the states. About 25% of the states have median income between \$45,000 and \$50,000.



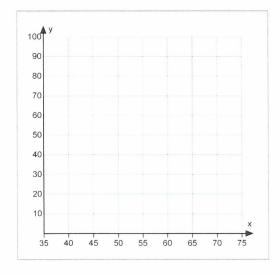
## 2.1A Activity

## **Cumulative Relative Frequency**

Example 1) President's Age at Inauguration

| Age   | Frequency | Relative frequency        | Cumulative frequency | Cumulative relative frequency |
|-------|-----------|---------------------------|----------------------|-------------------------------|
| 40-44 | 2         | 2/44 = 0.045, or 4.5%     | 2                    | 2/44 = 0.045, or 4.5%         |
| 45-49 | 7         | 7/44 = 0.159, or 15.9%    | 9                    | 9/44 = 0.205, or 20.5%        |
| 50-54 | 13        | 13/44 = 0.295, or $29.5%$ | 22                   | 22/44 = 0.500, or 50.0%       |
| 55-59 | 12        | 12/44=0.273,or27.3%       | 34                   | 34/44 = 0.773, or 77.3%       |
| 60-64 | 7         | 7/44 = 0.159, or 15.9%    | 41                   | 41/44 = 0.932, or 93.2%       |
| 65-69 | 3         | 3/44 = 0.068, or $6.8%$   | 44                   | 44/44 = 1.000, or 100%        |

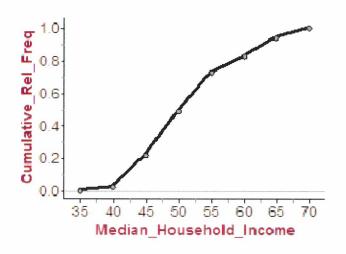
1) Use the above cumulative relative frequency table to create a cumulative relative frequency graph.



- 2) USE THE GRAPH TO ANSWER THESE QUESTIONS AND ANSWER IN CONTEXT:
- A) What percent of Presidents were between 55 and 60 when they were inaugurated?
- B) Was President Obama, who was inaugurated at 47 unusually young?
- C) Estimate and interpret the 65 percentile of the distribution
- D) Estimate the IQR?

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- b) What is the 25<sup>th</sup> percentile for this distribution? What is another name for this value?
- c) Estimate the IQR
- d) Where is the graph the steepest? What does this indicate about the distribution?