

SIMULATION STEPS

- ASSIGN
- RANDOMIZE
- SELECT include Record + EXCLUDE
- STOP
- CALCULATE

HOMEWORK:
COMPLETE THESE SIMULATIONS AND READ/TAKE NOTES ON SECTION 5.2

1) Law of large numbers - Tossing Coins (pages 284-288): "What is the probability of Heads?"

STEP 1: Clearly describe a process using your graphing calculator to simulate tossing a coin.

- 1) ASSIGN NUMBERS 0-4 TO HEADS AND NUMBERS 5-9 TO TAILS
- 2) USE TI84 RAND INT(0,9) TO SIMULATE EACH COIN TOS
- 3) RECORD H OR T
- 4) REPEAT 10 times, then 25 times, then 100 times
- 5) CALCULATE THE % HEADS AND NUMBER FOR THE LONGEST STREAK OF HEADS.

STEP 2: Complete the following simulations:

randInt(0,9,10)

1) Toss a coin 10 times and record your tosses (e.g. HTTHT...).
 The % heads was $\frac{3}{10} = 30\%$ What was the longest streak of heads? 2

T T H H T T H T T T H T T T T H H T H T 40%

randInt(0,9,25)

2) Toss a coin 25 times and record your tosses (e.g. HTTHT...).
 The % heads was $\frac{11}{25} = 44\%$ What was the longest streak of heads? 5

H T H H H H T T T T T H T H T H T
H T T H T T

randInt(0,9,100)

3) Toss a coin 100 times and record your tosses (e.g. HTTHT...).
 The % heads was $\frac{50}{100} = 50\%$ What was the longest streak of heads? 8

T H T T T H T T H H T H H H H H H H H
T H T T H H H T H T H H H T H H H T T H T
H T T T H T T H H T H H H T T T H T H H
T H T T H H T T T T H T T T H H H H H T T
H H T H T T T H H T H T T T

STEP 3: Conclusions:

a) What is the law of large numbers? IF WE OBSERVE MORE ^{AND} REPETITIONS OF ANY CHANCE PROCESS, THE PROPORTION OF TIMES THAT A SPECIFIC OUTCOME OCCURS APPROACHES A SINGLE VALUE, WHICH WE CALL THE PROBABILITY OF THAT OUTCOME.

b) How do you interpret a probability? ① OUTCOME OF A CHANCE PROCESS
② PROPORTION OF TIMES THE OUTCOME OCCURS IN A VERY LONG SERIES OF REPETITIONS.
③ NUMBER BETWEEN 0 (Never occurs) and 1 (always occurs)
* BEWARE OF SCIENTIFIC NOTATION ON CALCULATORS!

$.10E-3 = .0001$

2) Simulations – NASCAR Cards and Cereal Boxes (page 291):

STEP 1: Clearly describe a simulation process using your graphing calculator to answer:

QUESTION: What is the probability that it will take 23 or more boxes of cereal to get a full set of 5 NASCAR collectible cards?

TECHNOLOGY: You need to decide whether to use RANDINT() or RANDINTNOREP()

THERE CAN BE REPEATS

SIMULATION:

① ASSIGN: THERE ARE 5 TYPES OF CARDS SO DEFINE NUMBERS 1-5.

1 = GORDON

4 = PATRICK

2 = EARN HARDT JR

5 = JOHNSON

3 = STEWART

LOWEST # HIGHEST #

② RANDOMIZE: USE RandINT(1, 5, 100) TO SIMULATE BUYING THE BOXES OF CEREAL.

NUMBERS 1-5 represent the cards and 0, 6-9 are IGNORED

③ STOP & RECORD THE NUMBER OF BOXES UNTIL YOU GET ALL 5 CARDS

④ Repeat the simulation 20 times

EXAMPLE: (3)(5)(4)(2) 3 5 5 2 4 3 3 2 (1)

13 BOXES

STEP 2: Complete the simulation 20 times. Hint: circle winning cards & count number of cereal boxes.

- 1) (3) (5) (4) (2) 3 5 5 2 4 3 3 2 (1) 13 Boxes
- 2) (2) (4) (1) 4 (3) 2 1(5) 9 BOXES
- 3) (5) (2) (4) 2 (1) 4 2 (3) 8 BOXES
- 4) (4) (2) (5) (1) 5 (3) 6 BOXES
- 5) (2) (3) 3 2 (1) (4) (5) 7 Boxes
- 6) (5) (3) 5 5 (4) (1) 1 4 (2) 9 boxes
- 7) (1) 1 (3) 3 (2) (4) 3 (5) 9 boxes
- 8) (3) (5) (4) (2) 2 3 4 4 5 2 3 (1) 12 boxes
- 9) (2) (1) (3) (5) 3 1 (4) 7 boxes
- 10) (4) (2) (1) 2 (5) 5 2 1 1 4 4 1 (3) 13 boxes
- 11) (4) (2) 2 (5) (3) 2 3 2 2 (1) 10 boxes
- 12) (4) 4 (3) (5) (2) 4 3 (1) 8 boxes
- 13) (2) (5) (4) (1) 5 4 4 1 4 2 5 5 4 5 1 5 (3) 17 boxes
- 14) (1) (2) (3) (4) 2 1 2 (5) 8 boxes
- 15) (5) 5 (2) (4) 4 (1) 2 4 4 2 5 2 4 (3) 14 boxes
- 16) (2) (1) 2 1 1 (4) (3) (5) 8 boxes
- 17) (5) (3) 5 (4) 4 (2) 3 3 5 3 2 3 3 4 5 2 5 5 2 2 1 21 boxes
- 18) (3) (4) 3 (1) (2) 1 4 1 4 3 (5) 11 boxes
- 19) (1) (5) (3) 3 3 (4) (2) 7 boxes
- 20) (4) (2) 4 4 2 2 4 4 (3) 3 4 4 (5) 3 (1) 15 boxes

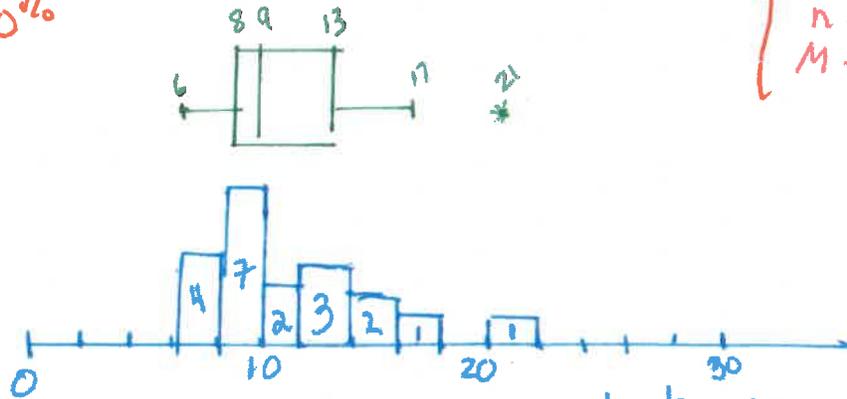


STEP 3: Create a graph of your results.

$P(\geq 23 \text{ or more boxes}) = \frac{0}{20} = 0\%$

Descriptive
STATS

STATS	
\bar{x}	= 10.6
s_x	= 3.9
n	= 20
M	= 9



Number of cereal boxes bought to get all 5 NASCAR cards

STEP 3: Clearly explain your conclusion.

Remember!
Hedging
Words

BASED ON THIS SIMULATION IT IS VERY ~~UNLIKELY~~ IT WOULD TAKE BUYING 23 BOXES TO GET THE 5 CARS.

IN THIS SIMULATION, WE NEVER HAD TO BUY MORE THAN 21 BOXES. SO OUR ESTIMATE OF THE PROBABILITY OF TAKING 23 OR MORE BOXES TO GET THE FULLSET IS ~~PROBABLY~~ 0.

THEREFORE, THE NASCAR FAN SHOULD BE SURPRISED ABOUT HOW MANY BOXES SHE HAD TO BUY.

AN COMMON ERROR

Hedging
Words

WHEN STUDENTS MAKE CONCLUSIONS, THEY OFTEN LOSE CREDIT FOR A CLAIM, ~~IF~~ ^{IF STATED} A DEFINITELY TRUE OR THE EVIDENCE PROVES THE CLAIM.

A BETTER RESPONSE WOULD BE TO SAY THERE IS SUFFICIENT EVIDENCE (OR THERE IS NOT SUFFICIENT EVIDENCE) TO SUPPORT A PARTICULAR CLAIM.