AP Statistics – 7.2 (2020 version)	Name:
Goal: Understanding Sample Proportion Sampling Distributions	Date:

I. Compare the means and standard deviations for our "Bean Activity"

Green Sheet: $\mu_{\widehat{p}} = p$ $\sigma_{\widehat{p}} = \sqrt{\frac{p(1-p)}{n}}$

1) SRS n=3. Find the mean and standard deviation.

$$P=1/2 \rightarrow L_{\beta}=1/2$$
 $G_{\beta}=\sqrt{\frac{15(.5)}{3}}=.289$

2) SRS n=5. Find the mean and standard deviation.

$$P=1/2 \rightarrow \mu \hat{p}=1/2$$
 $G\hat{p}=\sqrt{(.5)(.5)}=,224$

3) SRS n=20. Find the mean and standard deviation.

$$P = 1/2 \rightarrow \mu \hat{p} = 1/2$$
 $G \hat{p} = \sqrt{\frac{.5(.5)}{20}} = .112$

4) How do the means compare?

The means are the same.

Apris an unbiased estimator of the true population p

because by definition an unbiased estimator must Equal THE

population parameter

AS THE SAMPLE SIZE OF THE SRS INCREASES,

THE VARIABILITY DECREASES AND GO DECREASES.

II. Important Ideas - Sampling Distributions of \widehat{p}

#1 Pand
$$\hat{p}$$
 are 90 's

Mand X are averages.

Large Counts

IF THE SAMRING

DISTRIBUTION OF \hat{p}

is approx. normal:

 $\mu\hat{p} = p$
 $\eta(1-p) > 10$
 $\eta(1-p) > 10$

IF THE 10% CONDITION MET.

III. Sampling Distributions of \hat{p} (CYU on page 437):

ALWAYS DEFINE THE POPULATION PARAMETER (Tip: WRITE DIRECTLY FROM QUESTION)

P = TRUE PEUPORTION OF YOUNG ADULT INTERNET USERS (18-29) WHO WATCH ONLINE VIDEOS

- ① P=.75 → Mp=.75
- @ To calculate S.D, the independent condition
 must be met!

10% CONDITION - SRS [n=1,000], IT IS FAIR TO ASSUME
THE POPUlation is over 10,000 young adults.

$$G\beta = \sqrt{\frac{(.75)(.25)}{1,000}} = .0137$$

- (4) SRS n = 9,000

6p = \(\frac{(.75)(.25)}{900U} = .0046 \(\text{The SD decreased}\)

when n increased)

TIP: Do NOT skip any of these steps !!!!!!!!

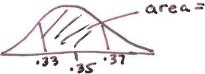
Example #1: A polling organization asks an SRS of 1500 first-year college students how far away their home is. Suppose that 35% of all first-year students actually attend college within 50 miles of home. What is the probability that the random sample of 1500 students will give a result within 2 percentage points of this true value?

1) What is the Population Parameter(s)?

P=TRUE % IST YEAR COLLEGE STUDENTS WHO LIVE WITHIN 50 miles

2) What Sample information is given?

Sketch Graph



- 4) What conditions must you check? Have they been met?
 - (1) IND EPENDENT SAMPLING W/O REPLACEMENT -1,500 < 10% (IST COLLEGE' STOPENTS)
 - NORMAL 1500 (.35) = 525 710/ 1500 (.65) = 975 7 10 /
- 5) Find the Mean and Standard Deviation. Clearly show your work.

$$M\beta = P = .35$$

$$G\beta = \sqrt{\frac{(.35)(.65)}{1500}} = .0123$$
STATE MODEL NN(.35,.0123)

6) Calculate the Z-Scores. Remember to label Z=

$$Z_L = \frac{.33 - .35}{.0123} = -1.63$$
 AND $Z_u = \frac{.37 - .35}{.0123} = 1.63$

7) Draw the standard normal graph N(0,1).



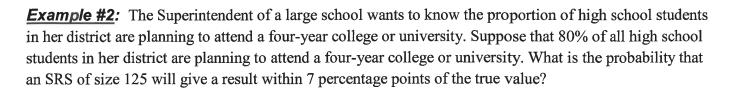
8) Estimate the probability with the 68-95-99.7 rule.

9) Restate the probability statement using the z-scores \rightarrow $P(-1.63 \pm Z \pm 1.63) = 8969$ & find the probability \rightarrow USE NGRMAL COF - NOCREOIT FOR CALC COMMANDS

10) Write conclusion (in context)

About 90% of all SRS'S OF SIZE 1,500 will give a result within 2% OF THE TRUE POPULATION Paremeter (35%) of 1st YEAR COLLEGE STUDENTS WHO LIVE within 50 miles of home.





- 1) What are the Population Parameter(s)? P=TRUE 00 OF HS students in this district planning to attend
 a 4 year college P=.80
- 2) What Sample information is given?

SRS
$$n=125$$
 $\hat{p}=?$

Sketch Graph.

3) State the probability of interest (in a probability statement). $(.73 \le 6 \le .87)$



- 4) What conditions must you check? Have they been met?
 - (1) INDEPENDENT SAMPLING W/O REPLACEMENT

* we must assume there are More than 1,250 HS. students in her district (10 x 125)

5) Find the Mean and Standard Deviation. Clearly show your work.

$$M\hat{\rho} = p = .8$$

$$C\hat{\rho} = \sqrt{\frac{(.8)(.2)}{12.5}} = .036 \longrightarrow NN(.8, .036)$$

6) Calculate the Z-Scores. Remember to label Z=

$$Z_{L} = \frac{.73 - .80}{.036} = -1.94$$
 AND $Z_{L} = \frac{.87 - .80}{.036} = 1.94$

11) Draw the standard normal graph N(0,1).



7) Estimate the probability with the 68-95-99.7 rule.



ABOUT 95% OF ALL SES'S OF SIZE 125 WILL GIVE A SAMPLE PROPORTION WITHIN 7 POINTS OF THE TRUE POPULATION PARAMETER (80%) OF H.S. students in this district who plan to attend a 4-yr college.