P(TYPE1 EREOR) = = = ,001

P=.05

FAIL TO REJECT HO AND

BRAND CHIPS.

CAN NOT CONCLUDE THAT

2140 M35 TA 27 W3 DUTS

SCHOOL PREFER NAME

## II. Type I and Type II Errors



## Definition:

If we reject  $H_0$  when  $H_0$  is true, we have committed a Type I error (FALSE POSITIVE)

If we fail to reject  $H_a$  when  $H_a$  is false, we have committed a Type II error (FALSE NEGATIVE)

 $\rightarrow$  Fill in the table: Type I error, Type II error, Power,  $\alpha$ ,  $\beta$ 

## Truth about the population

Ho true

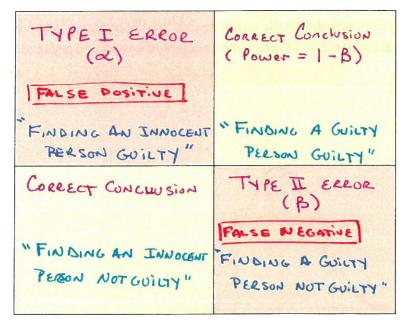
 $H_0$  false  $(H_a \text{ true})$ 

TRIAL ANALOGY

Reject Ho

Conclusion based on sample

Fail to reject  $H_0$ 



TYPE I ERROR & IS THE LEVEL OF SIGNIFICANCE. &= P(TYPE I ERROR)

TYPE I ERROR IS THE PROBABILITY OF REJECTING HOWHEN IT IS ACTUALLY TRUE

- \* TO REDUCE THE RISK OF A TYPE I ERRUR, SET & TO A LOWERLEVEL.

  \* BECREASING TYPE I ERROR INCREASES THE RISK OF A TYPE II END.

  \* TYPE I AND TYPE I ERRORS HAVE AN INVERSE RELATIONSHIP
- TYPE IT EREOR (B) IS THE PROBABILITY OF FAILING TO REJECT A FALSE HO
  - · FAILING TO REJECT HO MEANS THERE IS INSOFFICIENT EUIDENCE
    TO REJECT HO AND THUS HO COULD BE TRUE.

## 2003 Problem #2

When a law firm represents a group of people in a class action lawsuit and wins that lawsuit, the firm receives a percentage of the group's monetary settlement. That settlement amount is based on the total number of people in the group - the larger the group and the larger the settlement, the more money the firm will receive.

A law firm is trying to decide whether to represent car owners in a class action lawsuit against the manufacturer of a certain make and model for a particular defect. If 5 percent or less of the cars of this make and model have the defect, the firm will not recover its expenses. Therefore, the firm will handle the lawsuit only if it is convinced that more than 5 percent of cars of this make and model have the defect. The firm plans to take a random sample of 1,000 people who bought this car and ask them if they experienced this defect in their cars.

Scoring:

(a) Define the parameter of interest and state the null and alternative hypotheses that the law firm should test.

P = the proportion of all cars of the specific make and model that have the defect

EPI

$$H_0: P = .05$$
 $H_A: P > .05$ 

(b) In the context of this situation, describe Type I and Type II errors <u>and</u> describe the consequences of each of these for the law firm.

EPI

CONSEGNENCE: THE FIRM WILL NOT RECOVER ITS EXPENSES,
RESULTING IN A LOSS TO THE LAW FIRM

TYPE IT ERROR: FAIL TO REJECT HO WHEN HO IS FALSE

THAT IS ... THE FIRM WILL REFUSE TO HANDLE THE SUIT

WHEN IT REALLY SHOULD HAVE

EPI

TO TAKE THE CASE AND MAKE MONEY. Total: 14

Example "Faster fast food?" The manager of a fast-food restaurant want to reduce the proportion of drive-through customers who have to wait more than 2 minutes to receive their food once their order is placed. Based on store records, the proportion of customers who had to wait at least 2 minutes was p = 0.63. To reduce this proportion, the manager assigns an additional employee to assist with drive-through orders. During the next month the manager will collect a ndorn sample of drive-through times and test the following hypotheses:

$$H_{\theta}$$
: p = 0.63  
 $H_{a}$ : p < 0.63

where p = the true proportion of drive-through customers who have to wait more than 2 minutes after their order is placed to receive their food.

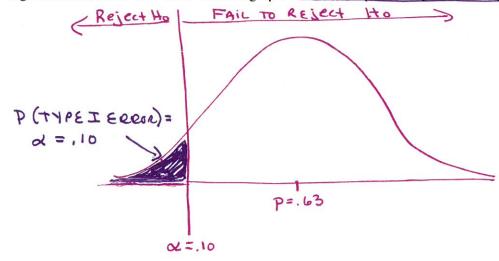
**Problem 1:** Describe a Type I and a Type II error in this setting and explain the consequences of each.

TYPE I ERROR would occur if the manager decides that the true proportion of drive through customers that have to wait at least 2 minutes has been reduced, when in fact it has not been reduced. Reject the A CONSEQUENCE is that the manager pays for an additional when p=.6-employee that he does not need.

Type II ERRUR woold occur if the manager decides the true Proportion of drive through customers that have to wait at least 2 minutes has NOT been reduced, when in fact the time had been reduced. Fail to

Reject Ho · A consequence is that the restaurent would NOT have an additional employee helping with the drive through, so they arenot providing faster service when they could roblem 2: Suppose that the manager decided to carry out this test using a random sample of 250 orders and a

significance level of  $\alpha = 0.10$ . Make a graph. What is the probability of a making a Type I error?



The Probability of a Type I ERRUR is 10% which Means We reject to when to is actually true. In this case, a Type I error occurs when the true proportion of costomers waiting at least 2 minutes remains p=.63, But we get a volve