

Midterm REVIEW 2016-17 (Chapters 1-4)

Evaluate each using the values given.

1) $y \cdot x \div 3 - x^2$; use $x = -3$, and $y = -3$

$$-6 \quad (-3)(-3) \div 3 - (-3)^2$$

$$9 \div 3 - (9)$$

$$3 - 9 =$$

$$\boxed{-6}$$

Simplify. Write in standard form.

2) $-6(10x - 3) + 5(3x - 7)$

$$\boxed{-45x - 17}$$

$$-60x + 18 + 15x - 35$$

Solve AND CHECK each equation.

3) $-(-3x - 4) = -7 + 4(x + 6)$

$$\{-13\}$$

$$3x + 4 = -7 + 4x + 24$$

$$\begin{array}{r} 3x + 4 = 4x + 17 \\ -3x \quad -3x \\ \hline 4 = x + 17 \\ -17 \quad -17 \\ \hline x = -13 \end{array}$$

C: $-(-3(-13)) = -7 + 4(-13 + 6)$
 $-35 = -35 \checkmark$

Write the equation in function form (Y=.....)

4) $3x - y = -6$

I isolate y

$$y = 3x + 6$$

$$-y = -3x - 6$$

$$\frac{-y}{-1} = \frac{-3x - 6}{-1}$$

$$\boxed{y = 3x + 6}$$

Draw a graph for each inequality.

5) $-6 < a$ *rewrite* $\rightarrow \boxed{a > -6}$

Open dot $\rightarrow >, <$

Write an inequality for each graph. Use the variable "X"

6)

$$\boxed{n \leq 6}$$

Closed Dot
 $\geq, \leq, =$

SOLVE each inequality. Circle the solution. Then GRAPH its solution.

7) $-6 - 3x < -(x - 4)$

$x > -5$

$$\begin{array}{r} -3x - 6 < -x + 4 \\ +x \quad +x \\ \hline -2x - 6 < 4 \\ +6 \quad +6 \\ \hline -2x < 10 \\ \div -2 \quad \div -2 \\ \hline x > -5 \end{array}$$

$$\boxed{x > -5}$$

Remember: When mult or divide the variable by a negative number, You MUST REVERSE THE SYMBOL.

SOLVE each compound inequality. Circle the solution. Then GRAPH its solution.

8) $-93 < -10x - 3 \leq 67$



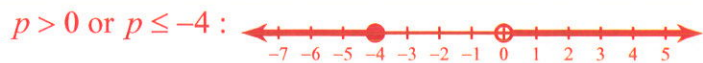
$$\begin{array}{r} -93 < -10x - 3 \leq 67 \\ +3 \quad \quad +3 \quad +3 \\ \hline -90 < -10x \leq 70 \\ \frac{-90}{-10} < \frac{-10x}{-10} \leq \frac{70}{-10} \end{array}$$

$9 > x > -7$

→ rewrite $-7 \leq x < 9$



9) $-1 + 8p > -1$ or $3p - 10 \leq -22$



$$\begin{array}{r} -1 + 8p > -1 \quad \text{OR} \quad 3p - 10 \leq -22 \\ +1 \quad \quad +1 \quad \quad \quad +10 \quad +10 \\ \hline 8p > 0 \quad \quad \quad 3p \leq -12 \\ \frac{8p}{8} > \frac{0}{8} \quad \quad \quad \frac{3p}{3} \leq \frac{-12}{3} \end{array}$$

$p > 0$ OR $p \leq -4$



Solve each inequality and graph its solution.

10) $|-2n + 8| \geq 2$

← THIS AN "OR"



$$\begin{array}{r} -2n + 8 \leq -2 \quad \text{OR} \quad -2n + 8 \geq 2 \\ -8 \quad -8 \quad \quad \quad -8 \quad -8 \\ \hline -2n \leq -10 \quad \quad \quad -2n \geq -6 \\ \frac{-2n}{-2} \leq \frac{-10}{-2} \quad \quad \quad \frac{-2n}{-2} \geq \frac{-6}{-2} \end{array}$$

$n \geq 5$ OR $n \leq 3$



11) $|5 - x| < 6$

← THIS IS AN "AND"



$$\begin{array}{r} -6 < 5 - x < 6 \\ -5 \quad -5 \quad \quad \quad -5 \\ \hline -11 < -x < 1 \\ \frac{-11}{-1} < \frac{-x}{-1} < \frac{1}{-1} \end{array}$$

$11 > x > -1$

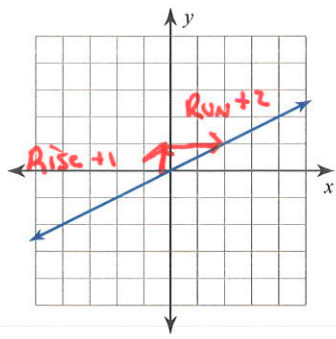
→ rewrite $-1 < x < 11$



Find the slope of each line.

12)

$\frac{1}{2}$



$m = \frac{\text{Rise}}{\text{Run}} = \frac{1}{2}$
 $M = \frac{1}{2}$

Find the slope of the line through each pair of points.

13) $(14, -16), (19, -10)$

$m = \frac{6}{5}$

$M = \frac{\Delta y}{\Delta x}$
 $M = \frac{-16 - (-10)}{14 - 19}$

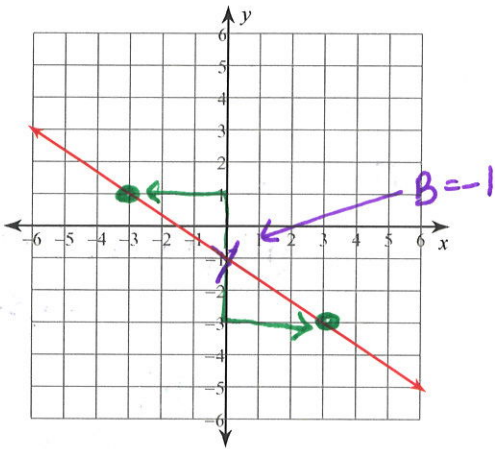
$M = \frac{-6}{-5}$

simplify.
 Keep as an improper fraction.

Sketch the graph of each line using slope and intercept. Clearly mark 3 points.

14) $y = -\frac{2}{3}x - 1$

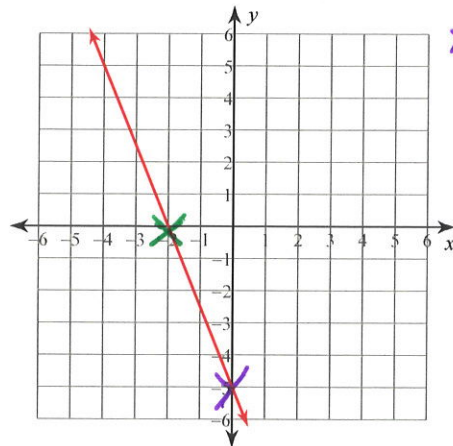
$M = -\frac{2}{3}$ $B = -1$



Sketch the graph of each line using intercepts. Label the x-intercept (X) and y-intercept (Y)

15) $5x + 2y = -10$

$\rightarrow (x, 0)$ $\rightarrow (0, y)$



X:
 $5x = -10$
 $x = -2$

Y:
 $2y = -10$
 $y = -5$

Write the point-slope form of the equation to describe the following lines. P/S $y - y_1 = m(x - x_1)$

16) through: $(5, -1)$, slope $= \frac{1}{3}$
 $y + 1 = \frac{1}{3}(x - 5)$

Write the slope-intercept form of the equation to describe the following lines.

17) Slope $= -\frac{2}{5}$, y-intercept $= -3$

$y = -\frac{2}{5}x - 3$ $y = mx + b$

18) through: $(-2, 5)$ and $(-1, -4)$

$y = -9x - 13$

STEP 1 FIND $m = \frac{\Delta y}{\Delta x} = \frac{5 - (-4)}{-2 - (-1)} = \frac{9}{-1}$

$m = -9$

STEP 2 pick a point and put in point-slope
 $y - 5 = -9(x + 2)$

STEP 3: PUT IN slope-intercept

$y - 5 = -9x - 18$
 $+5$ $+5$
 $y = -9x - 13$

Evaluate each function.

19) $f(x) = 2x^2 - x + 10$; Find *Substitute $x = -1$*

a) $f(-1) = 2(-1)^2 - (-1) + 10 = 2 + 1 + 10 = 13$

b) $f(0) = 2(0)^2 - 0 + 10 = 10$

c) $f(1) = 2(1)^2 - 1 + 10 = 2 - 1 + 10 = 11$

13, 10, 11

Construct a scatter plot.

- A) State if there appears to be a positive correlation, negative correlation, or no correlation.
 B) Identify if the relationship is linear, or non-linear.

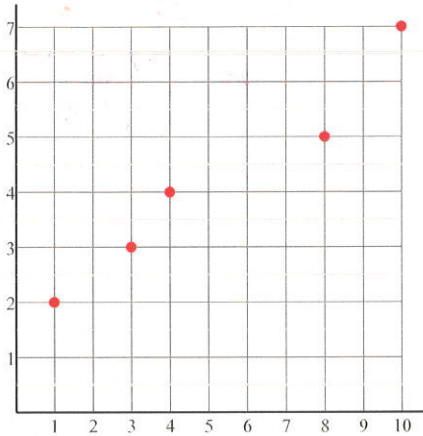
20)

X	Y
3	3
8	5

X	Y
10	7
8	5

X	Y
4	4

X	Y
1	2



- * Positive correlation
- * Linear relationship

Fit the Best Fit Line

- a) Construct a scatter plot.
 b) Find the equation of the line that best fits the data (round 2 decimals)
 c) Plot the Best Fit Line on the scatterplot:

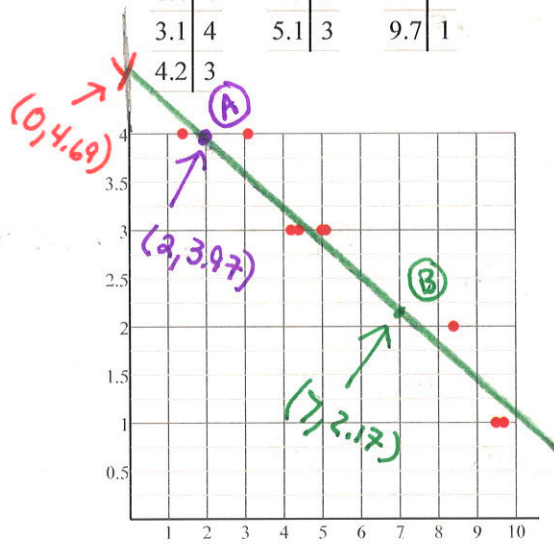
Label the y-intercept(Y);
 Label 2 points with their letters.
 Give the ordered pairs=
 pt A:(2, ___) & pt B:(7, ___)

21)

X	Y
1.4	4
1.4	4
3.1	4
4.2	3

X	Y
4.4	3
5	3
5.1	3

X	Y
8.4	2
9.5	1
9.7	1

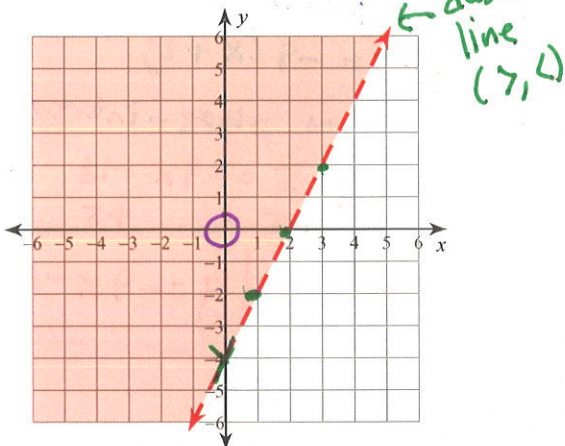


(A) $y = -.36(2) + 4.69 \rightarrow (2, 3.97)$
 (B) $y = -.36(7) + 4.69 \rightarrow (7, 2.17)$

Negative correlation
 $y = -0.36281x + 4.6939 \rightarrow y = -0.36x + 4.69$

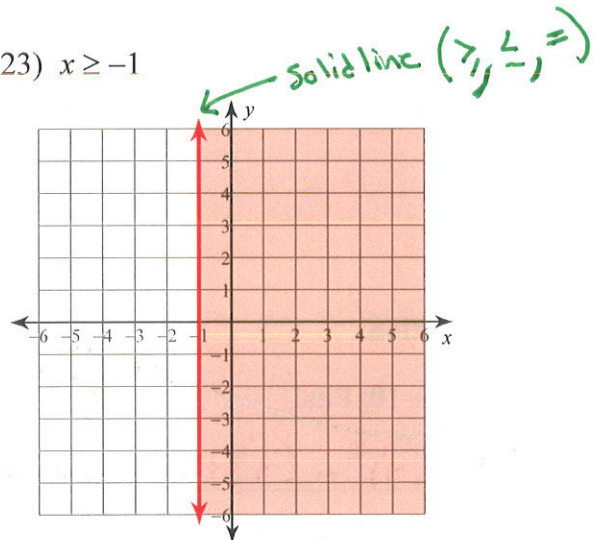
Sketch the graph of each linear inequality.

22) $y > 2x - 4$



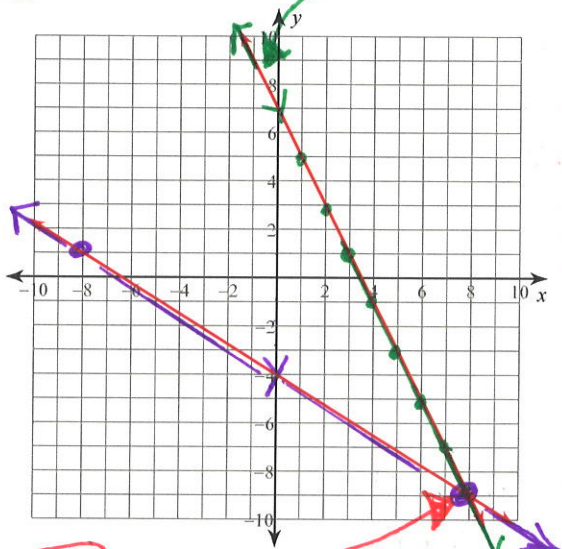
$T(0, -4) > -4 \rightarrow$
 Shade side with origin (0,0)

23) $x \geq -1$



Clearly graph the lines to solve the system.

24) (A) $2x + y = 7 \rightarrow y = -2x + 7$
 (B) $5x + 8y = -32$



$(8, -9)$

(B) $5x + 8y = -32$
 $-5x \quad -5x$

 $8y = -5x - 32$
 $\frac{8y}{8} = \frac{-5x}{8} - \frac{32}{8}$
 $y = -\frac{5}{8}x - 4$

Solve the system by graphing using the TICALC.

- a) Sketch the graph
- b) Identify the solution on the graph and label. Round the ordered pair to 2 decimals.
- c) Check algebraically.

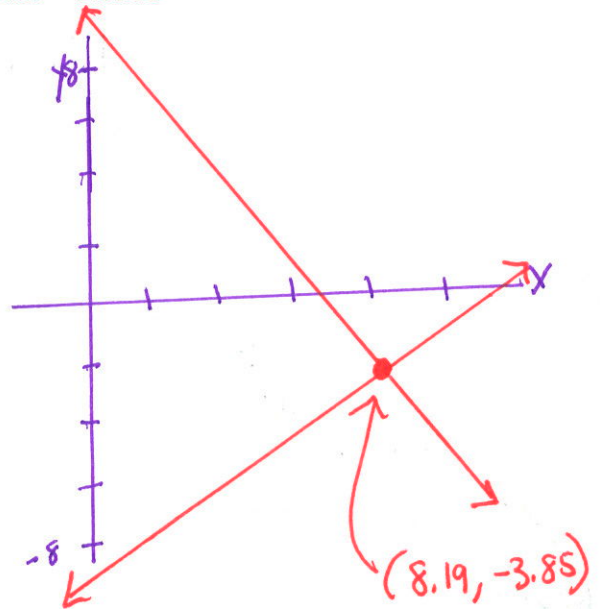
25) $y = 0.55x - 8.35$

$y = -\frac{14}{9}x + \frac{80}{9}$

ROUND CORRECTLY

(b) $(8.19, -3.85), (8.187, -3.846)$
 (c) $c: -3.85 = -3.8455$
 $c: -3.85 = -3.8511$

(a)



Solve system by substitution. Then Check!

26) $y = 2x - 8$
 $5x + 8y = -22$
 (2, -4)

$$5x + 8(2x - 8) = -22$$

$$5x + 16x - 64 = -22$$

$$21x - 64 = -22$$

$$\begin{array}{r} +64 \\ +64 \end{array}$$

$$\frac{21x}{21} = \frac{42}{21}$$

$$x = 2$$

FIND Y:

$$y = 2x - 8 = 2(2) - 8$$

$$y = -4$$

Solve each system by elimination (if possible). Clearly show your work!!!!

27) $-6x + y = -19$
 $6x - y = 19$

$$\begin{array}{r} -6x + y = -19 \\ 6x - y = 19 \\ \hline 0 = 0 \end{array}$$

Infinite number of solutions

Answer

28) $\begin{cases} 3x - 5y = 11 \\ 4x - 6y = 12 \end{cases}$

$$\begin{array}{r} (3x - 5y = 11) \times 4 \rightarrow 12x - 20y = 44 \\ (4x - 6y = 12) \times -3 \rightarrow -12x + 18y = -36 \\ \hline -2y = 8 \\ \hline -2 \quad -2 \\ \hline y = -4 \end{array}$$

(-3, -4)

FIND X:

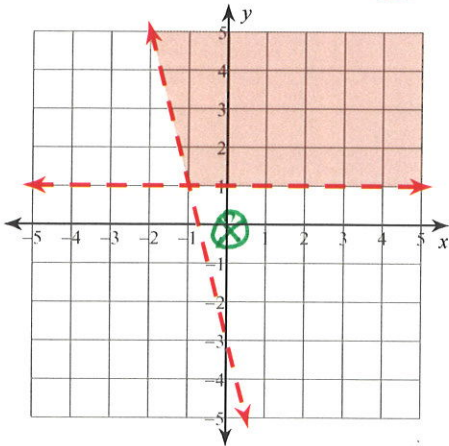
$$3x - 5(-4) = 11$$

$$3x + 20 = 11$$

$$\begin{array}{r} 3x + 20 = 11 \\ -20 \quad -20 \\ \hline 3x = -9 \\ \hline \frac{3x}{3} = \frac{-9}{3} \\ \hline x = -3 \end{array}$$

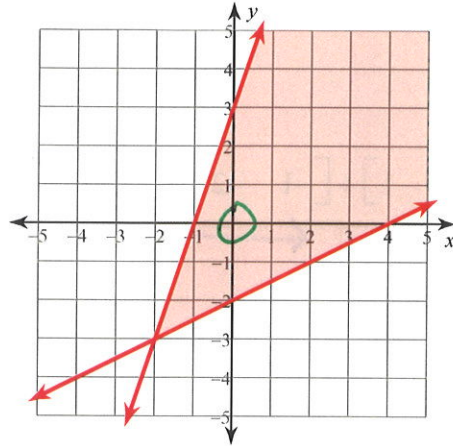
Sketch the solution to each system of inequalities.

29) $y > 1$ $0 > 1$ (F)
 $y > -4x - 3$ $0 > -3$ (F)



Test (0,0)

30) $y \leq 3x + 3$ $\rightarrow 0 \leq 3$ (T)
 $y \geq \frac{1}{2}x - 2$ $\rightarrow 0 \geq -2$ (T)



Simplify. Write "undefined" for expressions that are undefined.

31) $\begin{bmatrix} -4 & 2 & -5 \\ -1 & -2 & 5 \end{bmatrix} + \begin{bmatrix} 5 & -6 & -2 \\ -5 & -3 & -6 \end{bmatrix}$
 $\begin{bmatrix} 1 & -4 & -7 \\ -6 & -5 & -1 \end{bmatrix}$

32) $\begin{bmatrix} -4 & -1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} -4 & 3 \\ -5 & 6 \end{bmatrix}$
 $\begin{bmatrix} 0 & -4 \\ 6 & -6 \end{bmatrix}$

33) $\begin{bmatrix} 4 & 5 \\ -5 & -5 \end{bmatrix} \cdot \begin{bmatrix} -5 & 2 & 6 \\ 6 & -3 & 2 \end{bmatrix}$
 $\begin{bmatrix} 10 & -7 & 34 \\ -5 & 5 & -40 \end{bmatrix}$

34) $\begin{bmatrix} 4 & 6 \\ 3 & 5 \\ -4 & -5 \end{bmatrix} - 4 \begin{bmatrix} 5 & 6 \\ -1 & -1 \\ 4 & -1 \end{bmatrix}$
 $\begin{bmatrix} -16 & -18 \\ 7 & 9 \\ -20 & -1 \end{bmatrix}$

$$35) \begin{bmatrix} 2 & 1 \\ -1 & 0 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \\ -3 & 5 \end{bmatrix} \cdot \begin{bmatrix} 5 & -1 \\ -5 & -2 \end{bmatrix}$$

$$\begin{bmatrix} -30 & -9 \\ -5 & 1 \end{bmatrix}$$

$$36) \begin{bmatrix} -1 \\ 3 \end{bmatrix} \cdot \begin{bmatrix} 1 & 5 & 5 \end{bmatrix} \cdot \begin{bmatrix} -2 & 6 \\ 0 & -5 \\ 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -3 & 14 \\ 9 & -42 \end{bmatrix}$$

$$37) \begin{bmatrix} -2 & -6 & -3 & 1 \end{bmatrix} + \begin{bmatrix} -1 & -2 & -5 & -6 \end{bmatrix} + \begin{bmatrix} -4 & 6 & -3 & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -14 & -5 & -8 \end{bmatrix}$$

Solve the system using any method. Clearly show your work. Matrix Algebra Equation or solve with elimination method.

$$38) \begin{cases} -4x + 6z = -2 \\ 4x - 2y - 6z = 12 \\ -4x - 7y + 5z = 30 \end{cases}$$

$$(5, -5, 3)$$

Show this work

$$\begin{matrix} A & & X \\ \begin{bmatrix} -4 & 0 & 6 \\ 4 & -2 & -6 \\ -4 & -7 & 5 \end{bmatrix} & \begin{bmatrix} x \\ y \\ z \end{bmatrix} & = & \begin{bmatrix} -2 \\ 12 \\ 30 \end{bmatrix} \end{matrix}$$

$$X = [A]^{-1} [B]$$

Give answer:

① ordered pair $(5, -5, 3)$ OR

② Variables

$$x = 5$$

$$y = -5$$

$$z = 3$$