APSTATISTICS CHAPTER 5 - PROBABILITY REVIEW

 $[\Pi]$ A group of 50 college students were classified according to hair and eye color. The results are summarized in the joint frequency table below-

Cells	Tours			Marginel
Blue eyes Green eyes	Red hair 6	Blond hair 12	Brown hair	122 Totals
	reinel 16	70	14	50 = TT

- What is the probability that a randomly selected student has brown hair? (a)
- What is the probability that a randomly selected has red hair or brown hair? (b)
- What is the probability that a randomly selected student has red hair or green (c) eyes?
- What is the probability that a randomly selected student has red hair and blue (d)
- What is the probability that a randomly selected student with green eyes has blond (e) Restricted scample - Conditional Prob
- Are the two events "red hair" and "green eyes" independent? Show work to (f) support your conclusion.
 To see if independent create Bue 4223.27 GREEN 10/28=.36 8/28=.29

b) P(RH ORBH) = 16 +14 = 30 OR means "add"

c)
$$P(RH \text{ or } GE) = \frac{16}{50} + \frac{28}{50} - \frac{10}{50} = \frac{34}{50}$$

P(RHand BE) = 650

And means "mult inte

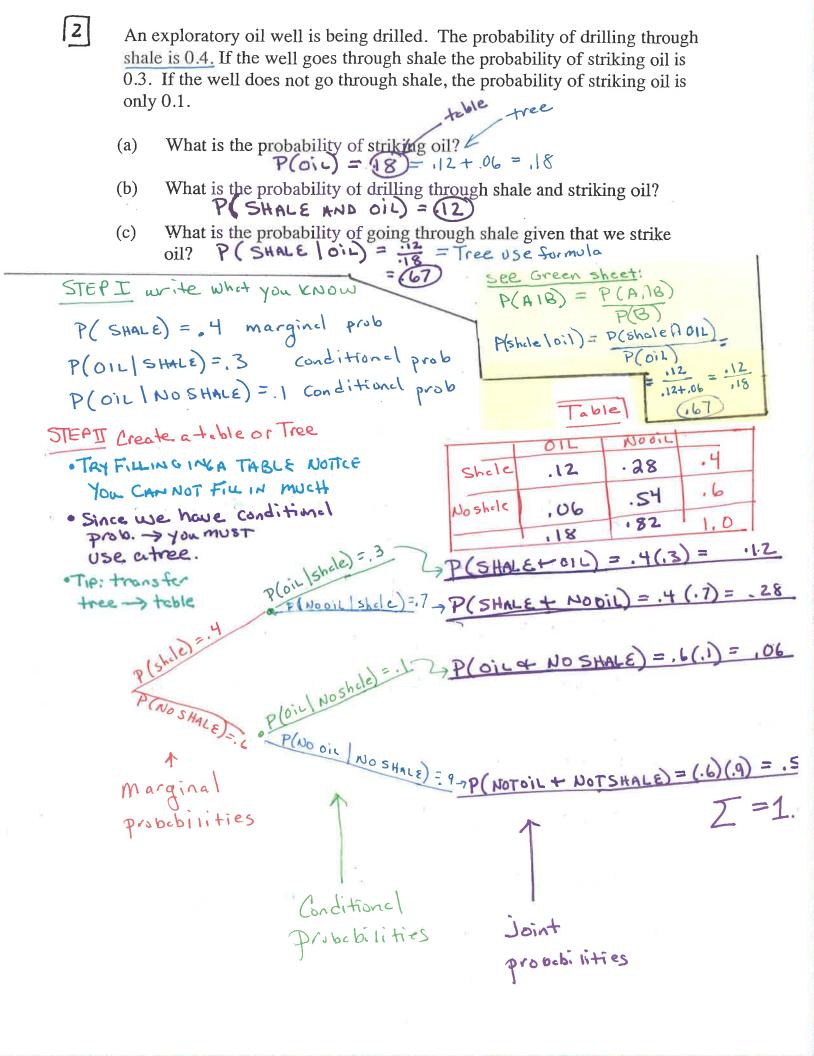
e) P(BH|GE) = 8 Conditional Probability

CELL/marginal

Tindependent P(AIB) = P(A)

10 = 16

P(RHIGE) = P(RH) P(GE|RH) = P(GE)



	BLOE	NOTBLUE	
PREGNANT	.038	,00 9	.04
NOT PREGNANT	.048	912	.96
10 V V V +	.086	,914	1.00

3	Medi-Mart has just come out with a new pregnancy test that registers blue (indicating a
4	pregnancy) in 95% of users who are pregnant. However, the new monitor also registers
	blue in 5% of the users who are not pregnant. Suppose that, in reality, only 4% of
	women using this test are pregnant.

- Construct a table or draw a tree diagram that reflects the situation, including (a) probabilities or counts.
- What is the probability that a randomly selected woman who uses this test gets a "blue" result?
- What is the probability that the woman actually is pregnant given that the test registers blue?

IDENTIFY PROBABILITIES GIVEN:

P(BLUE | PREG) = .95 P(BLUE I NOT PREG) = . 05 (Conditional) P(PREG) = .04 (marginal)

Since Conditional probabilities are given, need to start with a tree (then can convert to a table)

P(PREG and Blue) = .04 (.95) = .038 P(PREU and NotBlue) = .04 (.05)

Joint PROGRAGILITIES (Z=1.00)

NOW IT IS EASY TO CREATE TABLE TO ANSWER ?'S (See above)

b) P(BLUE) = (086) FROM TREE = 1038 + .048 = (086)

FROM TREE (USING GREEN SHEET) P(AIB) = P(ANB)

REPLACEMENT SAMPLING WITH OUT

4

Another hand. You pick three cards at random from a deck. Find the probability of each event described below.

- a) You get no aces.
- b) You get all hearts.

c) The third card is your first red card.

d) You have at least one diamond. P(Noace). P(Noace). $P(NoACE'S) = \frac{52-4}{52} = \frac{48}{52} \cdot \frac{47}{51} \cdot \frac{46}{50}$

P(ALL HEARTS) = 13 (12) (11) (50) = 1.013

P(300 CARDIS the 137 RED) = 26 - 25 - 26 - 50

P(atleast 1 diemond)

Shirts. The soccer team's shirts have arrived in a big box, and people just start grabbing them, looking for the right size. The box contains 4 medium, 10 large, and 6 extra-large shirts. You want a medium for you and one for your sister. Find the probability of each event

a) The first two you grab are the wrong sizes.

- b) The first medium shirt you find is the third one you check.
- The first four shirts you pick are all extra-large.
- d) At least one of the first four shirts you check is a medium.

GIV EN 4 medium Went amediums 20 SHIRTS

P(NOT M) . P(NOTM) = 16 . 15

(b) P(NOTM). P(NOTM). P(m) = 16 15 4 = 140

(C) P(XL) · P(XL) · P(XL) = $\frac{6}{20} \cdot \frac{5}{19} \cdot \frac{4}{18} \cdot \frac{3}{17} = 0.003$

P(at least 1 of 4 shirts is Medium) = 1 - (none are medium)
P(NM). P(NM). P(NM). P(NM)

1- (16)(15)(14)(13)=

NM = NOT medium

DISTOINT AND INDEPENDENCE iversity requires its biology majors to GIVEN P(STATS)

Eligibility. A university requires its biology majors to take a course called BioResearch. The prerequisite for this course is that students must have taken either a Statistics course or a computer course. By the time they are juniors, 52% of the Biology majors have taken Statistics, 23% have had a computer course, and 7% have done both.

a) What percent of the junior Biology majors are ineligible for BioResearch? Asked for %

b) What's the probability that a junior Biology major who has taken Statistics has also taken a computer course? (restricted Sample)

c) Are taking these two courses disjoint events? Explain.

 d) Are taking these two courses independent events? Explain. GIVEN P(STATS) = .52
P(Compoter) = .23
P(Stats and computer) = .07

CREATE A TABLE

COMPOTER

Y

N

10732 .4548 .52

N .1678 .3248 .48

123 .77 /.00

Use segmented bor
graph to see 50%

the relationship.
*Graphs NOT similar
when not independent.

Computer

a) P(IN ELIGIBLE) = P(NEITHER) = 32%)

b) P(Computer | Stats) = .07 = .135 on 13.5%

C) No. Taking the 2 courses is NoT disjoint (or mutually exclusive) because they have outcomes in common- 7% took both courses

d) The 2 courses are not independent because

Note: {P(Computee) = P(Computer) STATS) or P(STATS) = P(STAT) COMPUTER)

Note: {P(STAT) Computer) = .52 + .07 = .30

OR

have to!

Phone service. According to estimates from the federal government's 2003 National Health Interview Survey, based on face-to-face interviews in 16,677 households, approximately 58.2% of U.S. adults have both a landline in their residence and a cell phone, 2.8% have only cell phone service but no landline, and 1.6% have no telephone service at all.

* ARE HAVING A CELL PHONE
AND A LANDLINE
INDEPENDENT? EXPLAIN.

Given: P (Cell and Land) = .582
P (Cell ond NO LL) = .028
P (NO PHONE) = .016

YES NO

YES NO

YES NO

374 398 .016 379 .39

.956 .044 1.000

To check for independence: P(A) = P(A|B)

P(Cell) = P(CELL | Land)
61 = 1582
1610 = 1609

P(LANDLINE) = P(LL | CELL)

.956 = .582

.61

.956 ~ .954

Conclusion: Since the probabilities are about the same, it appears cell and lendlines are independent.

That is knowing someone owns a cell phone has no effect on the chance they have a land line and vice versa

Validate with a segmented bur groph Two cents

Landline No landline 188

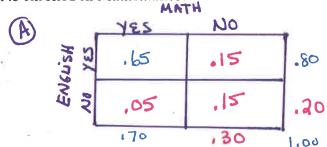
* Greats will be similer when independent



At a certain college 80% of the freshman are enrolled in English, 70% are enrolled in Mathematics, and 65% are enrolled in both courses. A freshman is to be randomly selected.

- Construct a two-way table showing this information. (a)
- What is the probability that a freshman is enrolled in English or Mathematics? (b)
- What is the probability that the freshman is enrolled in English, given that the (c) student is enrolled in Mathematics?

GIVEN P(ENG) = . 8 P (MATH) = .7 P (BOTH) = .65



- P(ENGLISH OR MATH) = P(ENG) + P(MATH) P(ENG and math) = .8 + .7 - .65 = (.85
- P(ENGLISH | MATH) = .65

Optic City sells six brands of digital cameras. Each brand is available in 2, 3, or 4 megapixels.

How many different digital cameras are sold by Optic City? (a)

Comera's = (#bronds) (# models) = 6(3)

- Make a tree diagram or a two-way table showing all of the different cameras. (b)
- What is the probability of randomly selecting any one of the digital cameras? (c) BRAND

		1	2	3	4	5	6
	1	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)	(46)
/apc	2	(2,1)	(2,2)	(4,3)	(2.4)	(2.5)	(2.6)
N	3	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)	(3,6)

