

## EVALUATE EXPRESSIONS

FIND THE VALUE OF THE EXPRESSION

## SOLVE EQUATIONS

FIND THE VALUE OF THE VARIABLE (x)

### 3.2

## Solve Two-Step Equations

Goal • Solve two-step equations.

Your Notes

To solve equations you isolate x.

### IDENTIFYING OPERATIONS FOR 2 STEP EQUATIONS

Identify the operations involved in the equation

$$3x + 7 = 19.$$

FIRST ALWAYS SIMPLIFY BOTH SIDES

① STEP 1: UNDO ADD / SUBTRACTION

② STEP 2: UNDO MULT / DIVISION

③ You must always check by substituting in the original equation.

### Example 1 Solve a two-step equation

Solve  $3x + 7 = 19$ .

Solution

$$\begin{array}{r} 3x + 7 = 19 \\ -7 \quad -7 \\ \hline \end{array}$$

$$\begin{array}{r} 3x = 12 \\ \div 3 \quad \div 3 \\ \hline \end{array}$$

$$x = 4$$

Write original equation.

Subtract 7 from each side.

Simplify.

Divide each side by 3

Simplify.

The solution is 4 circle it.

CHECK

$$3x + 7 = 19$$

$$3(\underline{4}) + 7 \stackrel{?}{=} 19$$

$$\underline{12} + 7 \stackrel{?}{=} 19$$

$$\underline{19} = 19 \checkmark$$

Write original equation.

Substitute 4 for x.

Multiply 3 by 4.

Simplify. Solution checks.

When solving a two-step equation, apply the inverse operations in the reverse order of the order of operations.

Checkpoint Solve the two-step equation. Check your solution.

$$1. \frac{r}{4} - 12 = -5$$

$$\frac{r}{4} + 12 = -5 + 12$$

$$\frac{r}{4} = 7$$

$$r = 28$$

$$2. 7k - 14 = 42$$

$$7k = 56$$

$$k = 8$$

Show all steps

C:  $\frac{28}{4} - 12 = -5$   
 $7 - 12 = -5$   
 $-5 = -5 \checkmark$

C:  $7(8) - 14 = 42$   
 $42 = 42 \checkmark$

← MINIMUM WORK FOR CHECKS

**Example 2** Solve a two-step equation by combining like terms

Solve  $4a + 3a = 63$ .

**Solution**

$4a + 3a = 63$  ← Write original equation.

Combine like terms.  $4a + 3a = 7a$

$$\frac{7a}{7} = \frac{63}{7}$$

Divide each side by 7.

$$a = 9$$

Simplify.

The solution is 9.

**CHECK**

$4a + 3a = 63$  Write original equation.

C:  $4(9) + 3(9) \stackrel{?}{=} 63$

$36 + 27 \stackrel{?}{=} 63$

$63 = 63 \checkmark$

ALWAYS SIMPLIFY BOTH SIDES FIRST

← Check in orig EQ

← START USE CALC FOR ARITHMETIC

← Show EQUATION checks

Checkpoint Solve the equation. Check your solution.

3.  $5z + 4z = 36$

$$9z = 36$$

$$z = 4$$

C:  $5(4) + 4(4) = 36$

$36 = 36 \checkmark$

4.  $5b - 2b = 9$

$$3b = 9$$

$$b = 3$$

C:  $5(3) - 2(3) = 9$

$15 - 6 = 9$

$9 = 9 \checkmark$

# 3.3

## Solve Multi-Step Equations

Goal • Solve multi-step equations.

Your Notes

**Example 1** Solve an equation by combining like terms

$$\text{Solve } 3t + 5t - 5 = 11.$$

Solution

$$\begin{array}{r} 8t - 5 = 11 \\ +5 \quad +5 \\ \hline 8t = 16 \\ \frac{8t}{8} = \frac{16}{8} \\ t = 2 \end{array}$$

The solution is 2.

Check:  $3(2) + 5(2) - 5 = 11$   
 $11 = 11 \checkmark$

SIMPLIFY

Write original equation.

Combine like terms.

Add 5 to each side.

Simplify.

Divide each side by 8.

Simplify.

STEP 1

ALWAYS  
SIMPLIFY  
BOTH SIDES

**Example 2** Solve an equation using the distributive property

$$\text{Solve } 5a + 3(a + 2) = 22.$$

$$5a + 3a + 6 = 22$$

Show All Steps

$$\begin{array}{r} 8a + 6 = 22 \\ -6 \quad -6 \\ \hline 8a = 16 \end{array}$$

$$\frac{8a}{8} = \frac{16}{8}$$

$$a = 2$$

$$C: 5(2) + 3(2+2) = 22$$

$$10 + 3(4) = 22$$

$$10 + 12 = 22$$

$$22 = 22 \checkmark$$

Checkpoint Solve the equation. Check your solution.

1.  $9d - 4d - 2 = 18$

$$\begin{array}{r} 5d - 2 = 18 \\ +2 \quad +2 \\ \hline 5d = 20 \\ \frac{5d}{5} = \frac{20}{5} \\ d = 4 \end{array}$$

C:  $9(4) - 4(4) - 2 = 18$   
 $36 - 16 - 2 = 18$   
 $18 = 18 \checkmark$

2.  $2x + 7(x - 3) = 6$

$$\begin{array}{r} 2x + 7x - 21 = 6 \\ 9x - 21 = 6 \\ +21 \quad +21 \\ \hline 9x = 27 \\ \frac{9x}{9} = \frac{27}{9} \\ x = 3 \end{array}$$

C:  $2(3) + 7(3 - 3) = 6$   
 $6 = 6 \checkmark$

3.  $40 = 2(10 + 4k) + 2k$

$$\begin{array}{r} 40 = 20 + 8k + 2k \\ 40 = 10k + 20 \\ -20 \quad -20 \\ \hline 20 = 10k \\ \frac{20}{10} = \frac{10k}{10} \\ k = 2 \end{array}$$

C:  $40 = 2(10 + 4(2)) + 2(2)$   
 $40 = 2(18) + 4$   
 $40 = 40 \checkmark$

**Example 3** Multiply by a reciprocal to solve an equation

Solve  $\frac{3}{4}(a - 5) = 9$ .

Solution

$$\begin{array}{r} \left(\frac{4}{3}\right) \frac{3}{4}(a - 5) = 9 \left(\frac{4}{3}\right) \\ 1(a - 5) = \frac{36}{3} \\ a - 5 = 12 \\ +5 \quad +5 \\ \hline a = 17 \end{array}$$

Write original equation.

Multiply each side by  $\frac{4}{3}$ .

2 WAYS TO SOLVE THIS PROBLEM

- ① DISTRIBUTE  $\frac{3}{4}$
- ② MULTIPLY BOTH SIDES BY THE RECIPROCAL

C:  $\frac{3}{4}(17 - 5) = 9$   
 $\frac{3}{4}(12) = 9$   
 $9 = 9 \checkmark$

Checkpoint Solve the equation. Check your solution.

5.  $\frac{1}{2}(4x - 2) = 7$

$$\begin{array}{r} 2x - 1 = 7 \\ +1 \quad +1 \\ \hline 2x = 8 \\ \frac{2x}{2} = \frac{8}{2} \\ x = 4 \end{array}$$

C:  $\frac{1}{2}(4 \cdot 4 - 2) = 7$   
 $\frac{1}{2}(16 - 2) = 7$   
 $\frac{1}{2}(14) = 7$   
 $7 = 7 \checkmark$



3.2 HW #'s 6-18 (EVEN)

- 6)  $G = 8$                       14)  $n = 21$   
 8)  $Q = 1$                       16)  $P = 6$   
 10)  $W = 20$                     18)  $X = 6$   
 12)  $Z = -12$

3.3 HW #'s 8-16 (EVEN), 19, 33, 38

- 8)  $Z = -5$   
 10)  $M = -7$   
 12)  $Z = 2$   
 14)  $M = 3$   
 16)  $C = 5$   
 19)  $D = 12$

38) KI: \$32.50 / ticket  
 plus \$3.30 / ticket  
 plus \$5.90 per order  
 Total spending = \$220.70

DEFINE VARIABLE:  
 $X = \#$  tickets bought

33 KI  $P = 288 \text{ inches} = 24 \text{ ft}$

$2+4=6$   
 $(x+4) \text{ ft}$   
 $4x \text{ ft}$   
 $4-2=8$   
 $10(x-1) \text{ ft}$   
 $6+8+10=24 \text{ ft}$

$P = 24 = (x+4) + 4x + 10(x-1)$   
 $24 = x+4 + 4x + 10x - 10$   
 $24 = 15x - 6$   
 $+6 \quad +6$   
 $30 = 15x \quad \textcircled{x=2}$   
 $15 \quad 15$

The sides are 6 ft, 8 ft, 10 ft

DEFINE EQ:  
 $(\$32.50 + \$3.30)X + 5.90 = 220.70$

$x = 6$

Bought 6 Tickets



# 3.4

## Solve Equations with Variables on Both Sides

**Goal** • Solve equations with variables on both sides.

EQUATIONS HAVE 3 TYPES OF SOLUTIONS  
Your Notes

- ① 1 SOLUTION  $x = \#$
- ② NO SOLUTION  $x = \emptyset$
- ③ ALL REAL NUMBERS

### VOCABULARY

Identity means that an EQUATION IS TRUE FOR ANY VALUE OF X.  
 SOLUTION  $\rightarrow$   $x = \text{all real numbers}$  or  $x = \mathbb{R}$

### Example 1 Solve an equation with variables on both sides

Solve  $15 + 4a = 9a - 5$ .

#### Solution

$$15 + 4a = 9a - 5$$

~~$-4a$~~     ~~$-4a$~~

---

$$15 = 5a - 5$$

$+5$     $+5$

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$$\frac{20}{5} = \frac{5a}{5}$$

$$a = 4$$

The solution is 4.

#### CHECK

$$15 + 4\left(\overset{a}{4}\right) \stackrel{?}{=} 9\left(\overset{a}{4}\right) - 5$$

$$15 + \frac{16}{31} \stackrel{?}{=} \frac{36}{31} - 5$$

$$31 = 31 \checkmark$$

Write original equation.

Subtract  $4a$  from each side.

Simplify.

① Add  $5$  to each side.

Simplify.

② Divide each side by  $5$ .

Simplify.

2 STEP EQUATION

In original equation. \*\*

Substitute  $4$  for  $a$ .

Multiply.

Solution checks.

Collect variables on one side of the equation and constant terms on the other to solve equations with variables on both sides.

① ALWAYS SIMPLIFY BOTH SIDES

② GET THE VARIABLE ON ONE SIDE

Your Notes

**Example 2** Solve an equation with grouping symbols

Solve  $4t - 12 = 6(t + 3)$ .

**Solution**

$4t - 12 = 6(t + 3)$  Write original equation.

$4t - 12 = 6t + 18$  \*Distributive property

$-4t \quad -4t$   
 $\frac{-12 = 2t + 18}{-18 \quad -18}$  \*Subtract  $4t$  from each side.

$\frac{-30 = 2t}{2 \quad 2}$  \*Subtract  $18$  from each side.

$t = -15$  \*Divide each side by  $2$ .

C:  $4(-15) - 12 = 6(-15 + 3)$   
 $-72 = -72 \checkmark$

**Checkpoint** Solve the equation. Check your solution.

1.  $3b + 7 = 8b + 2$

$\frac{-3b \quad -3b}{7 = 5b + 2}$   
 $\frac{-2 \quad -2}{5 = 5b}$   
 $\frac{5}{5} = \frac{5b}{5} \quad (b=1)$

C:  $3(1) + 7 = 8(1) + 2$   
 $10 = 10 \checkmark$

2.  $6d - 6 = \frac{3}{4}(4d + 8)$

$\frac{6d - 6 = 3d + 6}{-3d \quad -3d}$   
 $\frac{3d - 6 = 6}{+6 \quad +6}$   
 $\frac{3d = 12}{3 \quad 3} \quad (d=4)$

C:  $6(4) - 6 = \frac{3}{4}(4 \cdot 4 + 8)$   
 $24 - 6 = \frac{3}{4}(24)$   
 $18 = 18 \checkmark$

**Example 3** Identify the number of solutions of an equation

Solve the equation, if possible.

a.  $4x + 5 = 4(x + 5)$  Original equation

$4x + 5 = 4x + 20$  Distributive property

$-4x \quad -4x$   
 $5 \neq 20 \quad (F)$

$X = \text{NO SOLUTION}$  OR  $X = \emptyset$

When the variable drops out AND THE NUMBERS DO NOT EQUAL THEN THERE IS NO SOLUTION.

Check mentally but do not need to write!

b.  $6x - 3 = 3(2x - 1)$  Original equation

$6x - 3 = 6x - 3$  Distributive property

$-3 = -3 \quad (T)$

$X = \text{ALL REAL NUMBERS}$

When the variable drops out and the numbers are EQUAL THEN THERE IS AN INFINITE NUMBER OF SOLUTIONS.

Check

$x=0 \rightarrow$	$-3 = -3 \checkmark$	0 is A SOLUTION
$x=1 \rightarrow$	$3 = 3 \checkmark$	1 " " "
$x=2 \rightarrow$	$9 = 9 \checkmark$	2 " " "
$x=3 \rightarrow$	$15 = 15 \checkmark$	3 " " "
$x=4 \rightarrow$	$21 = 21 \checkmark$	4 " " "



**Your Notes**

ADD

15

$$4x - 3 = 3(x - 1)$$

$$\begin{array}{r} 4x - 3 = 3x - 3 \\ +3 \quad \quad +3 \end{array}$$

$$\begin{array}{r} 4x = 3x \\ -3x \quad -3x \end{array}$$

$$x = 0$$

$$\begin{array}{l} C: 4(0) - 3 = 3(0 - 1) \\ -3 = -3 \checkmark \end{array}$$

✓ **Checkpoint** Solve the equation, if possible.

$$3. \frac{1}{2}(4t - 6) = 2t$$

$$\begin{array}{r} 2t - 3 = 2t \\ -2t \quad \quad -2t \\ \hline -3 \neq 0 \end{array}$$

**T = NO SOLUTION**

$$\begin{array}{l} 2 \cdot \frac{1}{2}(4t - 6) = 2t \cdot 2 \\ 4t - 6 = 4t \end{array}$$

$$4. 10m - 4 = -2(2 - 5m)$$

$$\begin{array}{r} 10m - 4 = -4 + 10m \\ -10m \quad \quad -10m \\ \hline -4 = -4 \text{ (T)} \end{array}$$

**X = ALL REAL NUMBERS**

**BOOK ANSWER: IDENTITY**

**STEPS FOR SOLVING LINEAR EQUATIONS**

Step 1 Use the distributive property to remove any grouping symbols.

Step 2 Simplify the expression on each side of the equation.

Step 3 Use the properties of equality to collect the Variable terms on one side of the equation and the Constant terms on the other side of the equation.

Step 4 Use the properties of equality to solve for the variable.

Step 5 Check your solution in the original equation.



3.4 HW PG 157 #'s 4-14 (E), 18-26 (E), 41, 46

4)  $K=1$   
C:  $Z=2$  ✓

6)  $m=3$   
C:  $20=20$  ✓

8)  $P=-6$

10)  $H=3$   
C:  $8=8$  ✓

12)  $R=5$   
C:  $84=84$  ✓

14)  $n=7$   
C:  $45=45$  ✓

18)  $W=NO SOLUTION$

20)  $Z=NO SOLUTION$

22)  $X=-33$   
C:  $-656=-656$  ✓

24)  $Y=ALL REAL NUMBERS$

26)  $G=ALL REAL NUMBERS$

46) KI

$P=?$	$3x+7$
$4x-2$	$S=3(9)+7=(34)$

$S=4(9)-2=(34)$

$$\begin{array}{r} 4x-2 = 3x+7 \\ -3x \quad -3x \\ \hline x-2 = 7 \\ +2 \quad +2 \\ \hline x=9 \end{array}$$

$P=4(34)=136$

Perimeter = 136 UNITS

41)  $14 - \frac{1}{5}(J-10) = \frac{2}{5}(25+J)$   
 $14 - \frac{1}{5}J + 2 = \frac{2}{5}J + 10$

$$\begin{array}{r} -\frac{1}{5}J + 16 = \frac{2}{5}J + 10 \\ +\frac{1}{5}J \quad \quad +\frac{1}{5}J \\ \hline 16 = \frac{3}{5}J + 10 \\ -10 \quad \quad -10 \\ \hline 6 = \frac{3}{5}J \end{array}$$

$$\frac{5}{3} \cdot 6 = \frac{3}{5}J \left(\frac{5}{3}\right)^1$$

$$\frac{30}{3} = J$$

$J=10$

C:  $14 - \frac{1}{5}(10-10) = \frac{2}{5}(25+10)$   
 $\frac{2}{5}(35)^1$   
 $14=14$  ✓





# 3.5 Write Ratios and Proportions

**Goals** • Find ratios and write and solve proportions.

Your Notes

## VOCABULARY

**Ratio** The use of division to compare 2 quantities

**Proportion** 2 RATIOS THAT ARE EQUIVALENT. EXAMPLE  $\rightarrow \frac{1}{2} = \frac{20}{40}$

## RATIOS

1. A ratio uses Division to compare two quantities.
2. The ratio of two quantities,  $a$  and  $b$ , where  $b$  is not equal to 0, can be written in three ways:

$$\frac{a}{b} \quad a:b \quad \boxed{a \text{ to } b}$$

3. Each ratio is read "the ratio of  $a$  to  $b$ ".
4. Ratios should be written in Simplest form. EXAMPLE  $\rightarrow \frac{40}{60} = \frac{2}{3}$

### Example 1 Write a ratio

**Cell Phone Use** A person makes 6 long distance calls and 15 local calls in 1 month.

- Find the ratio of long distance calls to local calls.
- Find the ratio of long distance calls to all calls.

### Solution

a.  $\frac{\text{long distance calls}}{\text{local calls}} = \frac{6}{15} = \frac{2}{5}$

b.  $\frac{\text{long distance calls}}{\text{all calls}} = \frac{6}{6+15} = \frac{6}{21} = \frac{2}{7}$

**Your Notes**

- ✓ **Checkpoint** Shawn and Myra are selling tickets to their school's talent show. Shawn sold 36 tickets, and Myra sold 44 tickets. Find the specified ratio.

1. The number of tickets Shawn sold to the number of tickets Myra sold

$$\frac{\text{SHAWN}}{\text{MYRA}} = \frac{36}{44} = \boxed{\frac{9}{11}}$$

2. The number of tickets Myra sold to the number of tickets Shawn and Myra sold

$$\frac{\text{MYRA}}{\text{TOTAL}} = \frac{44}{80} = \boxed{\frac{11}{20}}$$

**Example 2** Solve a proportion

Solve the proportion  $\frac{y}{15} = \frac{3}{5}$ .

**Solution**

~~$$\frac{y}{15} = \frac{3}{5}$$~~

Write original proportion.

Use the same methods for solving equations to solve proportions with a variable in the numerator.

CROSS MULTIPLY  
AND DIVIDE

~~$$\frac{y}{15} = \frac{3}{5}$$~~

$$y = 3 \cdot \frac{15}{5}$$

$$\boxed{y = 9}$$

- ✓ **Checkpoint** Solve the proportion. Check your solution.

3.  ~~$\frac{9}{4} = \frac{c}{28}$~~

~~$$\frac{9}{4} = \frac{c}{28}$$~~

$$4c = 9 \times 28$$

$$\boxed{c = 63}$$

c:  $\frac{9}{4} = \frac{63}{28}$   
 $2.25 = 2.25$  ✓

4.  ~~$\frac{a}{32} = \frac{7}{8}$~~

~~$$\frac{a}{32} = \frac{7}{8}$$~~

$$8a = 7 \cdot 32$$

$$\boxed{a = 28}$$

c:  $\frac{28}{32} = \frac{7}{8}$   
 $.875 = .875$  ✓

Your Notes

**Example 3** Solve a multi-step problem

**Swimming Pool** A empty swimming pool is being filled with water. After 5 minutes the pool has 400 gallons of water. If the pool has a volume of 11,200 gallons, how long does it take to fill the empty pool?

**Solution**

**Step 1** Write a proportion involving two ratios that compare the amount of water in the pool to the amount of time.

$$\frac{400}{5} = \frac{11,200}{x}$$

← gallons                      ← minutes

Ratio is gallons to MINUTES

**Step 2** Solve the proportion.

$$\frac{400x}{400} = \frac{5(11,200)}{400}$$

$$x = 140$$

The pool is full after 140 minutes. OR 2 HOURS AND 20 MIN

✔ **Checkpoint** Complete the following exercise.

**Homework**

5. An Olympic sized pool has a volume of 810,000 gallons. If it is filled at the same rate as the pool in Example 3, how long will it take to fill the pool?

Rate:  $\frac{400 \text{ gallons}}{5 \text{ minutes}} = \frac{810,000 \text{ gal}}{M}$

M = # Minutes

$$\frac{400M}{400} = \frac{5(810,000)}{400}$$

$$M = 10,125 \text{ minutes}$$

$$\underline{\underline{168.75 \text{ hrs}}}$$





Key - 2014  
Revised so no Calc  
needed

## 3.6 Solve Proportions Using Cross Products

**Goal** • Solve proportions using cross products.

Your Notes

### VOCABULARY

Cross product

$$\frac{a}{b} = \frac{c}{d}$$

Cross Product:

$$a \cdot d = b \cdot c$$

NOTE IF THE CROSS PRODUCTS ARE EQUAL THEN IT IS A TRUE PROPORTION.

### CROSS PRODUCTS PROPERTY

**Words** The cross products of a proportion are EQUAL.

**Example**  $\frac{5}{6} = \frac{10}{12}$   $\frac{6}{5} \cdot 10 = \frac{60}{5} \cdot 12 = \frac{60}{5}$  They are equal

**Algebra** If  $\frac{a}{b} = \frac{c}{d}$  where  $b \neq 0$  and  $d \neq 0$ , then  $ad = bc$ .

Your Notes

**Example 1** Solve a proportion using cross products

Solve the proportion  $\frac{5}{y} = \frac{15}{75}$ .

**Solution**

$$\frac{5}{y} = \frac{15}{75}$$

Write original proportion.

$$15y = 15 \cdot 75$$

Cross products property

Simplify.

$$y = 25$$

The solution is 25

$$C: \frac{5}{25} = \frac{15}{75}$$

$$\frac{1}{5} = \frac{1}{5} \checkmark$$

← Reduce fractions

STEP I

K.I.:

3T food with 16oz water

80oz to feed plants

STEP II

VARIABLE

X = # of T of plant food

↑ must have UNITS

**Example 2** Write and solve a proportion

**Plant Food** To feed your plants, you need to mix 3 tablespoons of plant food with 16 ounces of water. If it takes 80 ounces of water to feed all of your plants, how many tablespoons of plant food are needed?

← DEFINE VARIABLE

**Solution**

**Step 3** Write a proportion involving two ratios that compare the amount of plant food with the amount of water.

$$\frac{3}{16} = \frac{x}{80}$$

← amount of plant food  
← amount of water

**Step 4** Solve the proportion.

$$\frac{16x}{16} = \frac{3 \cdot 80}{16}$$

Write proportion.

$$x = 15$$

Cross product property

Simplify.

STEP 5 WRITE ANSWER IN A SENTENCE

You need 15 tablespoons of plant food for 80 ounces of water.

**Your Notes**

C:  $\frac{1}{9} = \frac{25}{45} \Rightarrow 5$   
 $\frac{1}{9} = \frac{5}{45}$

✔ **Checkpoint** Solve the proportion. Check your solution.

1.  $\frac{5}{n} = \frac{25}{45}$   
 $\frac{5 \cdot 45}{25} = \frac{25n}{25}$   
 $5 = n$  (n=9)

2.  $\frac{6}{b} = \frac{3}{b-2}$   
 $6(b-2) = 3b$   
 $6b - 12 = 3b$   
 $-6b \quad -6b$   
 $-12 = -3b$   
 $4 = b$  (b=4)

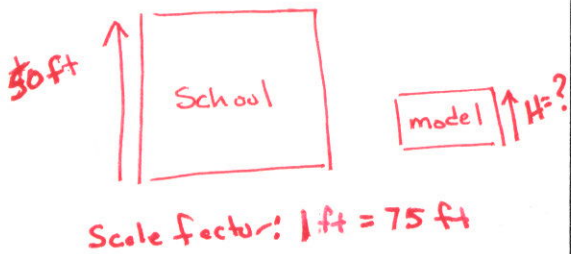
C:  $\frac{6}{4} = \frac{3}{4-2}$   
 $\frac{3}{2} = \frac{3}{2}$  ✓

3. In Example 2, suppose it takes **120 ounces** to feed all of the plants. How many tablespoons of plant food are needed?

$\frac{3}{16} = \frac{x}{120}$  →  $\frac{16x}{16} = \frac{3(120)}{16}$   
 $x = \frac{360}{16} = 22.5$

Need 22.5 tablespo. of plant food

KI:



Variable  
 H = height of the model (ft)

**Example 3** Use a scale model

**Scale Model** An architect creates a scale model of a school. The school is 50 feet high. The ratio of the model to the actual school is 1 foot to 75 feet. Estimate the height of the model.

**Solution**

Write and solve a proportion to find the height  $h$  of the scale model.

$\frac{H}{50} = \frac{1}{75}$  ← height of model (feet) / actual height (feet) } Ratio  
 ← scale factor  
 Cross products property  
 $\frac{75H}{75} = \frac{50}{75}$   
 Simplify.  
 $H = \frac{2}{3}$

The height of the scale model is  $\frac{2}{3}$  foot, or 8 inches.

$\frac{2}{3} \cdot 127$

✔ **Checkpoint** Complete the following exercise.

4. In Example 3, suppose the ratio of the model to the actual school is 1 foot to 100 feet. Estimate the height of the model.

$\frac{\text{MODEL}}{\text{ACTUAL}} = \frac{H}{50} = \frac{1}{100}$  ← scale factor

$\frac{100 \cdot H}{100} = \frac{50}{100}$

$H = \frac{1}{2} \text{ ft or } 6 \text{ in}$

HEIGHT OF THE MODEL IS 1/2 ft or 6 in





**N 3.6 HW** Pg 171 #'s 13, 19-25, 33-34

13)  $\frac{11}{w} = \frac{33}{w+24}$   
 $11(w+24) = 33w$   
 $264 = 22w$

$w = 12$

C:  $\frac{11}{12} = \frac{33}{12+24}$   
 $\frac{11}{12} = \frac{33}{36}$   
 $\frac{11}{12} = \frac{11}{12} \checkmark$

20)  $\frac{a}{9a-2} = \frac{1}{8}$   
 $8a = 9a - 2$   
 $-a = -2$   
 $a = 2$

19)  $\frac{7}{3} = \frac{2x+5}{x}$   
 $7x = 3(2x+5)$   
 $x = 15$

21)  $\frac{24}{5z+4} = \frac{4}{z-1}$   
 $24(z-1) = 4(5z+4)$   
 $4z = 40$   
 $z = 10$

22)  $\frac{c-8}{-2} = \frac{11-4c}{11}$   
 $11(c-8) = -2(11-4c)$   
 $11c - 88 = -22 + 8c$   
 $3c = 66$   
 $c = 22$

23)  $\frac{k-8}{7+k} = \frac{-1}{5}$   
 $5(k-8) = -1(k+7)$   
 $5k - 40 = -k - 7$   
 $6k = 33$   
 $k = 5.5$

24)  $\frac{2}{-3} = \frac{4v+4}{2v+14}$   
 $2(2v+14) = -3(4v+4)$   
 $4v+28 = -12v-12$   
 $16v = -40$   
 $v = -2.5$

25)  $\frac{m+1}{4} = \frac{3m+6}{7}$   
 $7(m+1) = 4(3m+6)$   
 $7m+7 = 12m+24$   
 $-17 = 5m$   
 $m = -3.4$

C:  $-0.6 = -0.6 \checkmark$

KS: **33**  $\frac{12 \text{ BISCUITS}}{2 \text{ C FLOUR}} = \frac{30 \text{ BISCUITS}}{x \text{ C FLOUR}}$   
 $x = 5$

**Need 5 CUPS FLOUR**

KS: **34**  $\frac{7.2 \text{ MIN}}{8 \text{ PHOTO'S}} = \frac{x \text{ MIN}}{20 \text{ PHOTO'S}}$   
 $x = 18$

**Will take 18 min. TO UPLOAD 20 PHOTO'S**

WP Proportion

$\rightarrow \frac{12}{2} = \frac{30}{x}$

WP Proportion  $\frac{7.2}{8} = \frac{x}{20}$

N 3.6 X HW

EXTRA CREDIT

Pg 172 #'s 35-39

KI:  $\frac{cm}{km}$

D = distance in km

35  $\frac{1 cm}{15 km} = \frac{6 cm}{D}$

DISTANCE = 90 km

36  $\frac{1 cm}{15 km} = \frac{3.2 cm}{D}$

D = 48

Distance is  
48 km

37  $\frac{1 cm}{15 km} = \frac{0.5 cm}{D}$

D = 7.5

Distance  
is 7.5 km

38  $\frac{1 cm}{15 km} = \frac{4.7 cm}{D}$

D = 70.5

DISTANCE is  
70.5 km

39 KI: MODEL 1m : 25m

EMPIRE STATE is 443.2 m

What is the height of the model?

H = Model height (m)

$$\frac{1}{25} = \frac{H}{443.2}$$

$$H = \frac{443.2 \times 1}{25}$$

$$H = 17.728$$

Model is 17.728 m tall

## 2 METHODS TO SOLVE PROPORTIONS

- ① PROPORTION METHOD
- ② WRITE AN EQUATION TO SOLVE

### **3.7** Solve Percent Problems

**Goal** • Solve percent problems.

Your Notes

#### **SOLVING PERCENT PROBLEMS USING PROPORTIONS**

**METHOD I**

You can represent "a is p percent of b" by using the proportion

$$\frac{a}{b} = \frac{p}{100}$$

OR

$$\frac{\text{IS}}{\text{OF}} = \frac{\%}{100}$$

where a is a part of the base b and  $\frac{P}{100}$  or  $p\%$ , is the percent

**METHOD I**

#### **Example 1** Find a percent using a proportion

What percent of 50 is 33?

#### **Solution**

Write a proportion when 50 is the base and 33 is part of the base.

$$\frac{33}{50} = \frac{P}{100} \quad \leftarrow \text{Write proportion.}$$

$$\cancel{50}P = \frac{33 \cdot \cancel{100}^2}{\cancel{50}}$$

$$P = 66\%$$

**SOLVE**  
Cross products property

33 is 66% of 50.

Don't forget % sign



METHOD I:  $\frac{IS}{OF} = \frac{?}{100}$

Your Notes

Checkpoint Use a proportion to answer the question.

1. What percent of 80 is 28?

$$\frac{P}{100} = \frac{28}{80} \Rightarrow \frac{80P}{80} = \frac{28 \cdot 100}{80} \Rightarrow P = 35\%$$

2. What percent of 90 is 36?

$$\frac{P}{100} = \frac{36}{90} \Rightarrow \frac{90P}{90} = \frac{36 \cdot 100}{90} \Rightarrow P = 40\%$$

METHOD II

THE PERCENT EQUATION

You can represent "a is p percent of b" by using the equation:

EQ:  $a = P\% \cdot b$

where a is a part of the base b and p% is the percent.

TRANSLATE

"IS" means =

"OF" means multiply

Variables

P = percent

N = number

Example 2 Find a percent using the percent equation

What percent of 250 is 100?

Write percent equation:  $P \cdot \frac{250}{250} = \frac{100}{250}$

SOLVE IT:  $P = \frac{100}{250} = \frac{2}{5} \%$  → decimals

Write decimal as a percent.  $P = .4$

100 is 40% of 250

CHECK with proportion method

$$\frac{P=40}{100} = \frac{100}{250}$$

$40 \cdot 250 = 100 \cdot 100$  Cross products  
 $10,000 = 10,000$  ✓

$\frac{2}{5}$   
divide

$5 \overline{) 2}$

Your Notes

WRITE

**Example 3** Find a part of a base using the percent equation

What number is 75% of 300?

**Solution**

$$N = .75 \cdot 300$$

Write percent equation.

$$N = 225$$

Change %'s to decimals !!

$$C: \frac{225}{300} = \frac{75}{100}$$

$$225(100) = 300(75)$$

$$22,500 = 22,500 \checkmark$$

225 is 75% of 300

✔ **Checkpoint** Use the percent equation to answer the question.

Check w/ proportion

3. What percent of 75 is 60?

$$P \cdot 75 = 60$$

$$\frac{P \cdot 75}{75} = \frac{60}{75} \stackrel{\div 3}{=} \frac{12}{15} \stackrel{\div 3}{=} \frac{4}{5}$$

$$P = 4/5 \rightarrow P = 80\%$$

$$C: \frac{80}{100} = \frac{60}{75}$$

$$80(75) = 60(100)$$

$$6,000 = 6,000 \checkmark$$

4. What number is 40% of 80?

$$N = .4 \cdot 80$$

$$N = 32$$

$$C: \frac{32}{80} = \frac{40}{100}$$

$$3,200 = 3,200 \checkmark$$

**Example 4** Find a base using the percent equation

25 is 12.5% of what number?

**Solution**

Write percent equation.

Change 12.5% → .125

$$25 = .125 \cdot N$$

$$N = 200$$

25 is 12.5% of 200.

$$C: \frac{12.5}{100} = \frac{25}{200}$$

$$2,500 = 2,500 \checkmark$$



Your Notes

✔ **Checkpoint** Use the percent equation to answer the question.

5. 60 is 25% of what number?

EQ →

$$60 = .25 \cdot N$$

$$\frac{60}{.25} = \frac{.25 \cdot N}{.25}$$

$$n = \frac{6000}{.25}$$

Proportion →

$$\frac{60}{N} = \frac{25}{100}$$

$$\frac{25N}{25} = \frac{60 \cdot 100}{25}$$

N = 240

6. 75 is 150% of what number?

EQ →

$$75 = 1.50 \cdot N$$

$$\frac{75}{1.50} = \frac{1.50 \cdot N}{1.50}$$

$$n = \frac{7500}{1.50}$$

Proportion →

$$\frac{75}{N} = \frac{150}{100}$$

$$\frac{150N}{150} = \frac{75 \cdot 100}{150}$$

$$n = \frac{750}{15} = \frac{150}{3}$$

$$n = \frac{150}{3}$$

N = 50

**TYPES OF PERCENT EQUATIONS**

Percent Problem	Example	Equation
① Find a percent.	What percent of 252 is 84?	$P \cdot 252 = 84$
② Find part of a base.	What number is 30% of 90?	$N = .30 \cdot 90$
③ Find a base.	16 is 20% of what number?	$16 = .20 \cdot N$

① Find a percent.

What percent of 252 is 84?

$$P \cdot 252 = 84$$

② Find part of a base.

What number is 30% of 90?

$$N = .30 \cdot 90$$

③ Find a base.

16 is 20% of what number?

$$16 = .20 \cdot N$$

IS → =  
OF → ×  
Change %'s to decimals

**Homework**



3.7 (EVENS)

Pg 179

(4)

$$\begin{aligned} & \text{EQ} \\ P \cdot 120 &= 66 \\ p &= .55 \end{aligned}$$

$$\begin{aligned} & \text{Proportion} \\ \frac{66}{120} &= \frac{P}{100} \end{aligned}$$

$$P = 55\%$$

(6)

$$\begin{aligned} N &= .60 \cdot 85 \\ N &= 51 \end{aligned}$$

$$\frac{60}{100} = \frac{N}{85}$$

(8)

$$\begin{aligned} 42 &= 2.00 \cdot N \\ N &= 21 \end{aligned}$$

$$\frac{200}{100} = \frac{42}{N}$$

(10)

$$\begin{aligned} P \cdot 225 &= 99 \\ P &= .44 \end{aligned}$$

$$\frac{P}{100} = \frac{99}{225}$$

$$P = 44\%$$

(12)

$$\begin{aligned} N &= .18 \cdot 150 \\ N &= 27 \end{aligned}$$

$$\frac{18}{100} = \frac{N}{150}$$

(14)

$$\begin{aligned} N &= .82 \cdot 215 \\ N &= 176.3 \end{aligned}$$

$$\frac{82}{100} = \frac{N}{215}$$

(16)

$$189 = .9 \cdot N$$

$$\frac{90}{100} = \frac{189}{N}$$

$$N = 210$$



## 3.8 Rewrite Equations and Formulas

**Goal** • Write equations in function form and rewrite formulas.

### Your Notes

FUNCTION FORM

$$y = m x + b$$

↑ slope                      ↑ y-intercept

### VOCABULARY

Function form IS THE SAME AS  $y = mx + b$

\* GIVEN AN EQUATION WITH X AND Y  
YOU ISOLATE Y ( $y = \underline{\quad}$ )

Literal equation are equations with  
2 OR MORE VARIABLES  
(AKA Letters)

### Example 1 Rewrite an equation in function form

Write  $2x + 2y = 10$  in function form.

#### Solution

Solve the equation for  $y$ .

$$2x + 2y = 10 \quad \leftarrow \text{Write original equation. ISOLATE } y$$

$$2y = -2x + 10 \quad \leftarrow \text{Subtract } 2x \text{ from each side.}$$

$$y = -x + 5 \quad \leftarrow \text{Divide each side by } 2. \text{ (ALL TERMS DIVIDE BY 2)}$$

The equation  $y = -x + 5$  is written in function form.

### Example 2 Solve a literal equation

Solve  $a + by = c$  for  $a$ .

#### Solution

$$a + by = c \quad \leftarrow \text{Write original equation. literal and solve for } a$$

$$a = c - by \quad \leftarrow \text{Subtract } by \text{ from each side.}$$

The solution is  $a = c - by$ .

**Your Notes**

KI

I = interest \$'s

P = investment \$'s

r = interest rate (% → decimal)

t = years

Formula:  $I = Prt$

**Example 3** Solve and use a formula

The interest  $I$  on an investment of  $P$  dollars at an interest rate  $r$  for  $t$  years is given by the formula  $I = Prt$ .

- a. Solve the formula for the time  $t$ .
- b. Use the rewritten formula to find the time it takes to earn \$100 interest on \$1000 at a rate of 5.0%.

**Solution**

a. 
$$\frac{I = Prt}{Pr} = \frac{Prt}{Pr}$$

$$\frac{I}{Pr} = t$$

$$t = \frac{I}{Pr}$$

Write original formula.  
Divide each side by  $Pr$ .

Solve for  $t$  to get a new formula

- b. Substitute \$100 for  $I$ , \$1000 for  $P$ , and 5% for  $r$  in the rewritten formula.

$$t = \frac{I}{Pr}$$
 Write rewritten formula.

$$t = \frac{100}{1000 \cdot .05}$$
 Simplify →  $t = \frac{100}{50}$

$$t = 2$$
 Simplify.

It will take 2 years to earn \$100 in interest.

Checkpoint Write the equation in function form.

1.  $2x + y = 5$   

$$y = -2x + 5$$

2.  $3 + 3y = 9 - 6x$   

$$y = -2x + 2$$

Checkpoint Complete the following exercises.

3. Solve  $ax + by = c$  for  $b$ .  

$$by = c - ax$$

$$b = \frac{c - ax}{y}$$

Variable Term is Constant Least

**Homework**

4. In Example 3, solve the equation for  $P$ . Find the investment  $P$  if  $I = \$400$ ,  $r = 4\%$  and  $t = 4$  years.

Write a new formula for  $P$

$$I = Prt$$

$$\frac{I}{rt} = \frac{Prt}{rt}$$

$$P = \frac{I}{rt}$$

Use the formula to answer?

$$P = \frac{I}{rt}$$

$$P = \frac{400}{.04(4)} = \frac{10000}{.16} = 2,500$$



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① LITERAL EQUATION (write sentence)

② To Solve  $I = prt$  for  $t$ .

① divide each side by  $pr$

② new formula

$$t = \frac{I}{pr}$$

Bonus

③

$$ax = bx - c$$

$$-bx - bx = -bx$$

$$ax - bx = -c$$

$$x(a-b) = -c$$

$$\frac{x(a-b)}{(a-b)} = \frac{-c}{(a-b)}$$

$$x = \frac{-c}{a-b}$$

④

$$a(x+b) = c$$

$$ax + ab = c$$

$$-ab - ab$$

$$\frac{ax}{a} = \frac{c-ab}{a}$$

$$x = \frac{c-ab}{a}$$

Cross multiply

⑤

$$c = \frac{x+a}{b}$$

$$b \cdot c = x+a$$

$$-a -a$$

$$x = bc - a$$

⑥

$$\frac{x}{a} = \frac{b}{c}$$

$$ab = \frac{bc}{c}$$

$$x = \frac{ab}{c}$$

Bonus

$$\textcircled{1} \quad \frac{x}{a} + b = c$$

$$\quad \quad \quad -b \quad -b$$

$$\frac{x}{a} = (c-b)$$

$$x = a(c-b)$$

$$\textcircled{8} \quad ax + b = cx - d$$

$$ax - cx + b = -d$$

$$\quad \quad \quad -b \quad -b$$

$$ax - cx = -b - d$$

$$x(a-c) = -b-d$$

$$\textcircled{11} \quad y = -2x + 7$$

$$x = \frac{-b-d}{a-c}$$

$$x = \frac{b+d}{c-a}$$

$$\textcircled{12} \quad 5x + 4y = 10$$

$$\quad \quad \quad -5x \quad -5x$$

$$4y = -5x + 10$$

$$\quad \quad \quad \frac{-5x}{4} \quad \frac{10}{4}$$

$$y = -\frac{5}{4}x + \frac{5}{2}$$

$$\textcircled{13} \quad y = -3x + 4$$

$$\textcircled{20} \quad V = lwh$$

$$\quad \quad \quad lh \quad lh \quad lh$$

$$w = \frac{V}{lh}$$

$$\textcircled{21} \quad S = 2B + Ph$$

$$\quad \quad \quad -2B \quad -2B$$

$$S - 2B = Ph$$

$$\quad \quad \quad \frac{S-2B}{P} = \frac{Ph}{P}$$

$$h = \frac{S-2B}{P}$$

$$\textcircled{22} \quad l = 24f$$

$$\quad \quad \quad \frac{l}{24} = \frac{24f}{24}$$

$$f = \frac{l}{24}$$