

5.3 Write Linear Equations in Point-Slope Form

Goal • Write linear equations in point-slope form.

2 FORMS OF LINEAR EQUATIONS THAT DESCRIBE A GIVEN LINE.

Your Notes

② P/S

VOCABULARY

Point-slope form MEMORIZE USE WHEN NOT GIVEN THE Y-INT.

$$y - y_1 = m(x - x_1)$$

- Coordinates of a given point (x_1, y_1)
- $m = \text{slope}$

① S/I

SLOPE - INTERCEPT FORM $y = mx + b$

$m = \text{slope}$
 $b = \text{y-intercept}$
 x and y variables

POINT-SLOPE FORM

The point-slope form of the equation of the nonvertical line through a given point (x_1, y_1) with a slope of m is

P/S $y - y_1 = m(x - x_1)$

Example 1 Write an equation in point-slope form

Write an equation in point-slope form on the line that passes through the point $(3, 2)$ and has a slope of 2.

Solution

$$y - y_1 = m(x - x_1)$$

Write point-slope form.

P/S

$$y - 2 = 2(x - 3)$$

Substitute 2 for m , 3 for x_1 , and 2 for y_1 .

point $(3, 2)$
 $M = 2$

Docheckpt #1

Your Notes

P/s: $y - y_1 = m(x - x_1)$

EXAMPLE 2

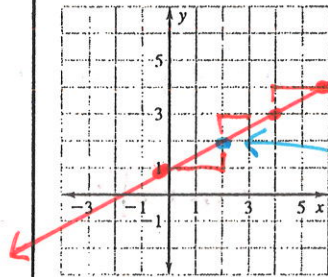
Graph the equation $y - 2 = \frac{1}{2}(x - 2)$.

* remember to take the opposite of the x_1 and y_1 .

Solution

Because the equation is in point-slope form, you know that the line has a slope of $\frac{1}{2}$ and passes through the point $(2, 2)$. $x_1 = 2$ $y_1 = 2$

Plot the point $(2, 2)$. Find a second point on the line using the slope. Draw a line through the points.



STEP I: plot point $(2, 2)$

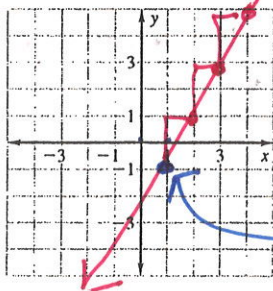
STEP II: use slope to find additional points
 $m = \frac{1}{2} = \frac{\text{Rise}}{\text{Run}}$

✓ **Checkpoint** Complete the following exercises.

- Write an equation in point-slope form of the line that passes through the point $(-3, 5)$ and has a slope of 4.

P/s: $y - 5 = 4(x - (-3))$

- Graph the equation $y + 1 = 2(x - 1)$.



$m = \frac{2}{1}$
 pt $(1, -1)$

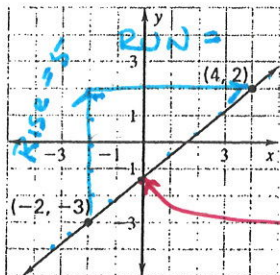
∞ number of points $\rightarrow \infty$ # OF P/S EQUATIONS
 $y - y_1 = m(x - x_1)$

1 y-intercept \rightarrow 1 S/I EQUATION ($y = mx + b$)

Your Notes

Example 3 Use point-slope form to write an equation

Write an equation in point-slope form of the line shown.



3 EQUATIONS TO DESCRIBE line.

P/S: $(4, 2) \quad y - 2 = \frac{5}{6}(x - 4)$

P/S: $(-2, -3) \quad y + 3 = \frac{5}{6}(x + 2)$

S/I: $b = -\frac{4}{3} \quad y = \frac{5}{6}x - \frac{4}{3}$

y-int is a fraction ($b = -\frac{4}{3}$)

Solution

Step 1 Find the slope of the line.

$$m = \frac{\text{Rise}}{\text{Run}}$$

$$m = \frac{5}{6} \quad \leftarrow \text{simplified}$$

Step 2 Write the equation in point-slope form.

You can use either given point.

Method 1 Use $(-2, -3)$.

Method 2 Use $(4, 2)$.

$$y - y_1 = m(x - x_1)$$

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = \frac{5}{6}(x - (-2))$$

$$y - 2 = \frac{5}{6}(x - 4)$$

Notice SIGNS become Positive

CHECK Check that the equations are equivalent by writing them in slope-intercept form.

$$y \frac{+3}{-} = \frac{5}{6}x + \frac{5}{3}$$

$$y \frac{-2}{+2} = \frac{5}{6}x - \frac{10}{3}$$

$$y = \frac{5}{6}x - \frac{4}{3}$$

$$y = \frac{5}{6}x - \frac{4}{3}$$

S/I

S/I

Same
 $y\text{-int} = b = -\frac{4}{3} = -1\frac{1}{3}$

Scrapping
 $1\frac{2}{3} - 3 = -1\frac{1}{3}$

Scrapping
 $-3\frac{1}{3} + 2 = -1\frac{1}{3} = -\frac{4}{3}$

WRITING EQUATIONS WITH 2 POINTS GIVEN.

5.2 Use Linear Equations in Slope-Intercept Form

(CONT.)

Goal • Write an equation of a line using points on the line.

Example 4 Write an equation given two points

Given 2 points →

Write an equation of the line that passes through $(2, -3)$ and $(-2, 1)$.

Solution

Step 1 Calculate the slope.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x} = \frac{-3 - 1}{2 - (-2)} = \frac{-4}{4} \quad \boxed{m = -1}$$

STEP 2 PUT IN POINT SLOPE FORM.

PICK EITHER POINT. Use the slope and the point

$\boxed{(2, -3)}$

$$y - y_1 = m(x - x_1)$$

P/S $\boxed{y + 3 = -1(x - 2)}$

You can also find the y-intercept using the coordinates of the other given point.

Step 3 Write an equation of the line. IN SLOPE INTERCEPT (WHEN ASKED)

Write slope-intercept form.

S/I $\boxed{y = -x - 1}$

$$y + 3 = -x + 2$$

S/I $\boxed{y = -x - 1}$

What is a 3RD EQUATION TO DESCRIBE THIS LINE?

P/S $(-2, 1)$ $\boxed{y - 1 = -1(x + 2)}$

Your Notes

Checkpoint Complete the following exercise.

2. Write an equation for the line that passes through $(-8, -13)$ and $(4, 2)$.

$$m = \frac{\Delta y}{\Delta x} = \frac{-13 - 2}{-8 - 4} = \frac{-15}{-12} \quad \boxed{m = 5/4}$$

① P/s $(4, 2) \rightarrow y - 2 = \frac{5}{4}(x - 4)$

② S/I

$$y - 2 = \frac{5}{4}x - 5$$

$$y = \frac{5}{4}x - 3$$

③ P/s $y + 13 = \frac{5}{4}(x + 8)$

3. Write an equation for the line that passes through $(-3, 4)$ and $(1, -2)$.

$$m = \frac{\Delta y}{\Delta x} = \frac{4 - (-2)}{-3 - 1} = \frac{6}{-4} \quad \boxed{m = -3/2}$$

① P/s $(-3, 4) \rightarrow y - 4 = -\frac{3}{2}(x + 3)$

② S/I

$$y - 4 = -\frac{3}{2}x - 9/2$$

$$y = -\frac{3}{2}x - 1/2$$

③ P/s $(1, -2) \rightarrow y + 2 = -\frac{3}{2}(x - 1)$

scribble
 $-4 \frac{1}{2} + 4 = -\frac{1}{2}$

HOW TO WRITE EQUATIONS IN SLOPE-INTERCEPT FORM $y = mx + b$

1. Given slope m and y-intercept b . then plug

$m + b$ into S/I EQ $\boxed{y = mx + b}$

2. Given slope m and one point.

(a) plug m and (x_1, y_1) into P/s
 $y - y_1 = m(x - x_1)$

(b) Use algebra to put into $y = mx + b$

3. Given two points.

(a) Use the points to find the slope $m = \frac{\Delta y}{\Delta x}$

(b) Pick a point and plug into P/s
 $y - y_1 = m(x - x_1)$

(c) Use algebra to put into $y = mx + b$

STEP 1
To find slope

① Given a graph
 $m = \frac{\text{Rise}}{\text{Run}}$

② Given 2 points
 $m = \frac{\Delta y}{\Delta x}$

5.3 (cont.)

Writing Equations for Horizontal and Vertical Lines

Your Notes:

- The equation of a **HORIZONTAL LINE** is $y = b$ where $b = y \text{ intercept}$ and the slope is Zero.
- The equation of a **VERTICAL LINE** is $x = a$ where $a = x \text{ intercept}$ and the slope is UNDEFINED.

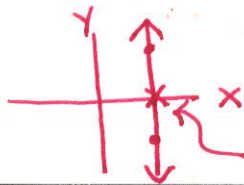
EXAMPLE 1

- Write the equation of the line that goes through the points (5, -2) and (5, 2)

STEP I: FIND $m = \frac{\Delta y}{\Delta x} = \frac{-2-2}{5-5} = \frac{-4}{0}$ $\boxed{m = \text{UNDEFINED}}$

$\boxed{x = 5}$

STEP II Sketch a Graph



X INTERCEPT $x = 5$

STEP 3 ALL VERTICAL LINES HAVE THE EQ $\boxed{x = a}$ where $a = x \text{ int}$

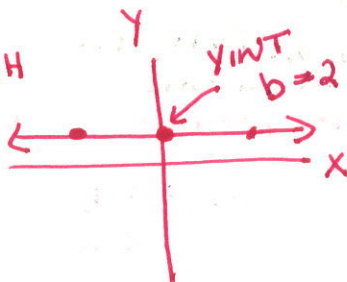
EXAMPLE 2

- Write the equation of the line that goes through the points (-3, 2) and (3, 2)

STEP I FIND $m = \frac{\Delta y}{\Delta x} = \frac{2-2}{-3-3} = \frac{0}{-6}$ $\boxed{m = 0}$

$\boxed{y = 2}$

STEP II SKETCH



y int $b = 2$

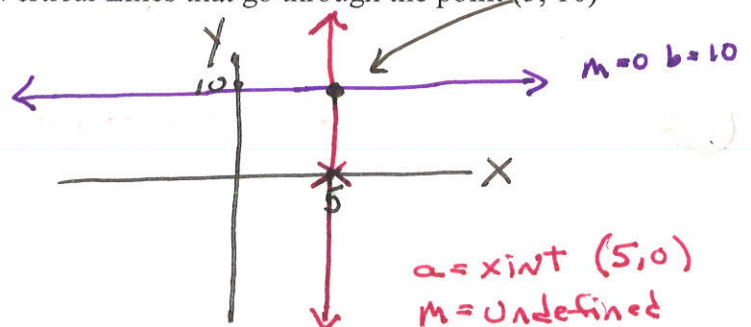
STEP III Fill in $y = mx + b$
 $m = 0$ $b = 2$
 $y = 0x + 2$
 $\boxed{y = 2}$

EXAMPLE 3

- Write the equation of for the Horizontal and Vertical Lines that go through the point (5, 10)

HORIZONTAL LINE $\boxed{y = 10}$

VERTICAL LINE $\boxed{x = 5}$



$m = 0$ $b = 10$

$a = x \text{ int } (5, 0)$
 $m = \text{Undefined}$
 $b = \text{None}$