

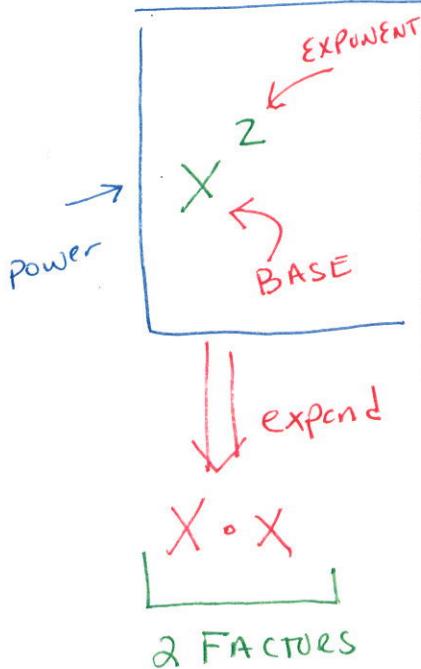


# Evaluate Expressions

**Goal** • Evaluate algebraic expressions and use exponents.

## Your Notes

An algebraic expression is also called a variable expression.



## VOCABULARY

Variable is a letter ( $x, y, a, b, \dots$ )

THAT REPRESENTS A NUMBER.

Algebraic expression is a collection of numbers, variables, operations (+, -, ×, ÷) AND SYMBOLS OF INCLUSION (), {}, {}

Evaluating an expression means to find the value of the expression

"EVALUATE EXPRESSIONS"

Power	FACTORS: NUMBERS OR VARIABLES
Base	MULTIPLIED TOGETHER
Exponent	FACTORS ARE SEPARATED BY MULT. SIGNS

"SOLVE EQUATIONS"

## ALGEBRAIC EXPRESSIONS

Algebraic Expression	Meaning	Operation
$7t$ <small>← implied mult</small>	7 times $t$	<u>Multiply</u>
$\frac{x}{20}$	FRACTIONS MEAN → Division	
$y - 8$	→ Subtraction	
$12 + a$	→ Addition	

## Your Notes

To evaluate an expression, substitute a number for the variable, perform the operation(s), and simplify.

### Example 1 Evaluate algebraic expressions

Evaluate the expression when  $n = 4$ .

a.  $11 \bullet n = 11 \times 4$  Substitute 4 for  $n$ .  
 $\uparrow 11n = \underline{44}$  ← EVALUATE

Given Expression

DO NOT USE  $\times$  FOR MULTIPLICATION

HW

Write the problem →  
Show Substitution →  
Evaluate →

Checkpoint Evaluate the expression when  $y = 8$ .

1. $7y$ $7(8)$ <u>56</u>	2. $y \div 2$ $8 \div 2$ <u>4</u>	3. $10 - y$ $10 - 8$ <u>2</u>	4. $y + 6$ $8 + 6$ <u>14</u>
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### Example 2 Read and write powers

Write the power in words and as a product. ← (did not say EVALUATE)

Power

Words

Product of factors

a.  $12^1$

twelve to the first power

$12 \leftrightarrow 12^1$

b.  $2^3$

two to the third power,

EXPAND AS A PRODUCT

$2 \cdot 2 \cdot 2$

or two cubed

c.  $(\frac{1}{4})^2$

one fourth to the second power, or one fourth squared

$\frac{1}{4} \cdot \frac{1}{4}$

d.  $a^4$

a to the 4<sup>TH</sup> power

$a \cdot a \cdot a \cdot a$

## Your Notes

## Checkpoint Write the power in words and as a product.

$\textcircled{5} 2^5$	$\textcircled{6} \left(\frac{1}{3}\right)^2$	$\textcircled{7} (10)^3$
WORDS → 2 to the 5 <sup>TH</sup> 2 · 2 · 2 · 2 · 2 $\textcircled{32}$	1/3 SQUARED $\frac{1}{3} \cdot \frac{1}{3} =$ $\textcircled{\frac{1}{9}}$	10 CUBED $10 \cdot 10 \cdot 10 =$ $\textcircled{1,000}$
Evaluate! (to find the value of the expression)		

## Example 3 Evaluate powers

Evaluate the expression.

a.  $y^3$  when  $y = 3$

**Solution**

$$\begin{aligned} a. y^3 &= \underline{(3)^3} \\ &= \underline{3 \cdot 3 \cdot 3} \\ &= \underline{\underline{27}} \end{aligned}$$

USE ( )'s when substituting to do order of operations

Substitute 3 for  $y$ .

Correctly

mentally expand

EVALUATE means find the VALUE of the expression

## Checkpoint Evaluate the expression.

## Homework

8.  $t^2$  when  $t = 3$

$(3)^2 =$

$\textcircled{9}$

9.  $m^5$  when

$m = \frac{1}{2}$

$\left(\frac{1}{2}\right)^5$

$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$

$\textcircled{\frac{1}{32}}$

Show substitution



mentally expand

# 1.2

## Apply Order of Operations

**Goal** • Use the order of operations to evaluate expressions.

### Your Notes

WARNING

Be careful using  
P E M D A S

### ORDER OF OPERATIONS

To evaluate an expression involving more than one operation, use the following steps.

Step 1 Evaluate expressions inside GROUPING SYMBOLS

Step 2 Evaluate POWERS

Step 3 MULTIPLY and divide from left to right.

Step 4 Add and SUBTRACT from left to right.

- ① ( )'s IN → OUT
- ② EXPONENTS
- ③  $\times, \div$  L → R
- ④ +, - L → R

### Example 1 Evaluate Expressions

Evaluate the expression  $30 \times 2 \div \underline{2^2} - 5 =$

EVALUATE:

$$\begin{aligned} 30 \times 2 \div \underline{2^2} - 5 &= \\ \underline{60 \div 4} - 5 &= \\ 15 - 5 &= \end{aligned}$$

(10)

Show work  
clearly +  
GO DOWN  
Not ACROSS

**Your Notes****Checkpoint** Evaluate the expression.

1. $10 + 3^2 =$ $10 + 9 =$ $\underline{19}$	2. $16 - \underline{2^3} + 4 =$ $16 - 8 + 4 =$ $\underline{8+4} =$ $\underline{\underline{12}}$
3. $28 \div \underline{2^2} + 1 =$ $\underline{28 \div 4} + 1 =$ $7+1 =$ $\underline{\underline{8}}$	4. $4 \cdot \underline{5^2} + 4 =$ $4 \cdot 25 + 4 =$ $100 + 4 =$ $\underline{\underline{104}}$

**Example 2** Evaluate expressions with grouping symbols

Evaluate the expression.

Grouping symbols such as parentheses ( ) and brackets [ ] indicate that operations inside the grouping symbols should be performed first.

a.  $6(9 + 3) =$   $6(\underline{12}) =$

$$= \underline{\underline{72}}$$

b.  $50 - (3^2 + 1) =$   $50 - (\underline{9+1}) =$   
 $50 - 10 =$

$$= \underline{\underline{40}}$$

c.  $3[5 + (5^2 + 5)] =$   $3[\underline{5 + (25 + 5)}] =$   
 $3[\underline{5 + 30}] =$

$$3(35) =$$

$$= \underline{\underline{105}}$$

START  
WITH THE  
INSIDE  
( )'S  
AND WORK  
OUT

## Your Notes

✓ **Checkpoint** Evaluate the expression.

5.  $6(3 + 3^2)$

$$\begin{aligned} 6(3+9) &= \\ 6(12) &= \\ \textcircled{72} & \end{aligned}$$



6.  $2[(10 - 4) \div 3]$

$$\begin{aligned} 2(6 \div 3) &= \\ 2(2) &= \\ \textcircled{4} & \end{aligned}$$

**Example 3** Evaluate an algebraic expression

Evaluate the expression  $\frac{12k}{3(k^2 + 4)}$  when  $k = 2$ .

**Solution**

$$\frac{12k}{3(k^2 + 4)} = \frac{12(2)}{3[(2)^2 + 4]}$$

**STEP I**

Substitute 2 for  $k$ . Use  $( )$  for substitutions

**STEP II** EVALUATE EXPRESSION

EVALUATE power.

*Fractions*

$$\begin{aligned} &= (1) \text{ simplify the numerator } 12 \cdot 2 = 24 \\ &\quad (2) \text{ simplify the denominator } 3[4+4] = 24 \\ &= \frac{24}{24} \\ &= \boxed{1} \end{aligned}$$

Simplify the fraction !!

Domentally

✓ **Checkpoint** Evaluate the expression when  $x = 3$ .

## Homework

7.  $x^3 - 5$

$$\begin{aligned} (3)^3 - 5 &= \\ 27 - 5 &= \\ \textcircled{22} & \end{aligned}$$

8.  $\frac{6x + 2}{x + 7}$

$$\begin{aligned} \frac{6(3)+2}{3+7} &= \\ \frac{20}{10} &= \textcircled{2} \end{aligned}$$



# Write Expressions

## Your Notes

**Goal** • Translate verbal phrases into expressions.

### VOCABULARY

Verbal model (used in this textbook) use words to describe the problem. This should be a mental step.

Rate **IS A FRACTION THAT COMPARES 2 QUANTITIES MEASURED IN DIFFERENT UNITS**

Unit rate **IS A RATE PER 1 GIVEN UNIT IN THE DENOMINATOR**

Ex] Simplify above rate: **50 miles/hour**

**EXAMPLE**  
Rate =  $\frac{400 \text{ miles}}{8 \text{ hours}}$

**UNIT RATE**

### TRANSLATING VERBAL PHRASES

Operation	Verbal Phrase	Expression
Addition	The <u>sum</u> of 3 and a number $n$	$3+n$
Subtraction	The <u>difference</u> of 7 and a number $a$ .	$7-a$
Multiplication	Five <u>times</u> a number $y$	$5y$
Division	The <u>quotient</u> of a number $a$ and 6	$\frac{a}{6}$

**QUANTITY means ( )'s**

**IS means EQUAL**

**OF means MULTIPLY**

Order is important when writing subtraction and division expressions.

order makes a difference

order matters

## Your Notes

The words "the quantity" tell you what to group when translating verbal phrases.

### Example 1 Translate verbal phrases into expressions

Translate the verbal phrase into an expression.

#### Verbal Phrase

- 6 less than the quantity  
8 times a number  $x$
- 2 times the sum of 5  
and a number  $a$
- The difference of 17 and  
the cube of a number  $n$

#### Expression

$$8x - 6$$

$$2(5+a)$$

$$17 - n^3$$

ONLY USE ()'S  
IF NEEDED!!!

### Checkpoint Translate the verbal phrase into an expression.

- The product of 5 and the quantity 12 plus a number  $n$

$$5(12+n)$$

- The quotient of 10 and the quantity a number  $x$   
minus 3

$$\frac{10}{x-3} \text{ or } 10/(x-3)$$

Be careful!  
~~10/x-3~~ wrong

### Example 2 Use a verbal model to write an expression

Food Drive You and three friends are collecting canned food for a food drive. You each collect the same number of cans. Write an expression for the total number of cans collected.

#### Solution

Step 1 mentally think of a verbal model:

Amount of cans  $\times$  Number of people

Step 2 Translate the verbal model into an algebraic expression.

$$C \cdot 4$$

An expression that represents the total number of cans is  $4C$ .

## KEY INFORMATION

4 people collect  
the same #  
of cans

## DEFINE VARIABLE

$C = \#$  of cans  
↑

DO NOT FORGET  
UNITS

# DAY 2

## Your Notes

### Key Info

Example 2

PLUS Divide into  
2 Food Banks

3. In Example 2, suppose that the total number of cans collected are distributed equally to 2 food banks. Write an expression that represents the number of cans each food bank receives.

$$\begin{array}{c} \xrightarrow{\text{Total cans}} \\ \frac{4C}{2} \end{array} \xrightarrow{\text{simplify}} \boxed{2C}$$

2 FOOD BANKS

## Example 3 Find a unit rate

Three gallons of milk cost \$9.15. Find the unit rate.

### Solution

- ① write as a rate  
② divide to find the unit rate

$$\frac{\$9.15}{3 \text{ gallons}} = \frac{\$3.05}{1 \text{ GALLON}}$$

The unit rate is  $\$3.05 \text{ per gallon}$  or  $\$3.05/\text{GAL}$

Scratch Paper

$$\begin{array}{r} 3.05 \\ \underline{3) 9.15} \\ -9 \quad \downarrow \\ \hline 15 \quad \downarrow \\ 15 \quad \downarrow \\ 0 \end{array}$$

answers

## Checkpoint Find the unit rate.

4.  $\frac{420 \text{ miles}}{3 \text{ hours}} =$

5.  $\frac{\$12}{3 \text{ ft}^2} =$

6.  $\frac{20 \text{ cups}}{8 \text{ people}} =$

### Homework

$140 \text{ miles/hr}$

$\$4/\text{ft}^2$

$\frac{20}{8} = \frac{10}{4} = \frac{5}{2}$

$2.5 \text{ cups/person}$   
or  
 $2\frac{1}{2} \text{ cups/person}$

RATES

UNIT RATES

# 14

## Write Equations and Inequalities

**Goal** • Translate verbal sentences into equations or inequalities.

Your Notes

IMPORTANT DEFINITION!

"SOLVE  
EQUATIONS  
AND  
INEQUALITIES"

### VOCABULARY

Open sentence ARE EQUATIONS AND INEQUALITIES

#### Equation

2 EXPRESSIONS CONNECTED WITH AN EQUAL SIGN

#### Inequality

2 EXPRESSIONS CONNECTED WITH  $>$ ,  $\geq$ ,  $<$ ,  $\leq$ ,  $\neq$

Solution of an equation IS THE NUMBER(s) THAT MAKE THE EQUATION TRUE

Solution of an inequality IS THE SET OF ALL NUMBERS THAT MAKE THE INEQUALITY TRUE

### EXPRESSING OPEN SENTENCES

#### Symbol Meaning

$a = b$  a is EQUAL to b

$a < b$  a is less than b

$a \leq b$  a is less than or EQUAL TO b

$a > b$  a is greater than b

$a \geq b$  a is greater than or EQUAL TO b

$a \neq b$  a is NOT EQUAL TO b

### EXAMPLE

①  $x < 5$

"5 is NOT A solution"

②  $x \leq 5$

"5 IS a solution"

**Example 1** Write equations and inequalities

ONLY USE ()'S  
IF NEEDED!

Write an equation or an inequality.

## Verbal Sentence

## Equation or Inequality

- The sum of three times a number  $a$  and 4 is 25.
- The quotient of a number  $x$  and 4 is fewer than 10.
- A number  $n$  is greater than 6 and less than 12.

$$3a + 4 = 25$$

$$\frac{x}{4} < 10$$

$$6 < n < 12 \quad \text{or}$$

$$n > 6 \text{ AND } n < 12$$

Sometimes two inequalities are combined. For example, the inequalities  $a < b$  and  $b < c$  can be combined to form the inequality  $a < b < c$ .

**Example 2** Check possible solutions

Check whether 2 is a solution of the equation or inequality.

## Equation or Inequality

## Substitute

## Conclusion

- $7x - 8 = 9$        $7(2) - 8 \stackrel{?}{=} 9$   
 $6 \neq 9$
- $4 + 5y < 18$        $4 + 5(2) \stackrel{?}{<} 18$   
 $14 < 18$

EVALUATE EACH SIDE

2 is NOT a solution.

EVALUATE EACH SIDE

2 IS a solution.

✓ **Checkpoint** Check whether the given number is a solution of the equation or inequality.

write problem

Show substitution

Check

1. $6r + 1 = 25$ $r = 4$ $6(4) + 1 = 25$ $25 = 25$ (4 is a solution)	2. $x^2 - 5 > 10$ $x = 5$ $(5)^2 - 5 > 10$ $25 - 5 > 10$ $20 > 10$ (5 is a solution)	3. $7a < 21$ $a = 6$ $7(6) < 21$ $42 < 21$ (6 is NOT a solution)
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Your Notes

**Example 3** Use mental math to solve an equation

Solve the equation using mental math.

a)  $n + 6 = 11$

b)  $\frac{b}{11} = 3$

Think of an equation as a question when solving using mental math.

SOLVE

Equation "Think"

a)  $n + 6 = 11$  What number plus 6 equals 11?

(n=5)

Check

5 + 6 = 11

11 = 11 ✓

BY SUBSTITUTING THE SOLUTION INTO THE ORIGINAL EQUATION!

SOLVE:

b)  $\frac{b}{11} = 3$

(b=33)

CHECK:

c)  $\frac{33}{11} = 3$

3 = 3 ✓

✓ Checkpoint Solve the equation using mental math. CHECK!!!!

Mentally →  
Solve

How to Do Homework  
 (A) Write Problem  
 (B) Circle Solution  
 (C) Check

4.  $x + 9 = 14$

(x=5)

5.  $5t - 4 = 11$

(t=3)

6.  $\frac{y}{4} = 15$

(y=60)

c:  $5+9=14$

14 = 14 ✓

c:  $5(3)-4=11$

$15-4=11$   
 $11=11$

c:  $\frac{60}{4}=15$

$15=15$  ✓

② Check in original equation.  
 MAKE SURE TO LABEL CHECK.



# Use a Problem Solving Plan

**Goal** • Use a problem solving plan to solve problems.

## Your Notes

### A PROBLEM SOLVING PLAN

Use the following four-step plan to solve a problem.

Step 1 Read and Understand Read the problem carefully. Identify what you want to know and what you want to find out. Read

STEPS { make a plan      Decide on an  
2-4 { approach to solving the problem.

Step 5 Solve the problem Carry out your plan. Try a new approach if the first one isn't successful.

Step 6 Look back and Check that your answer is reasonable.

### Example 1 Read a problem and make a plan

You have \$7 to buy orange juice and bagels at the store. A container of juice costs \$1.25 and a bagel costs \$.75. If you buy two containers of juice, how many bagels can you buy?

Solution:

KI: \$7 to spend  
\$1.25 - juice  
\$.75 - bagel  
2 containers of juice

Variable:

$B = \# \text{ bagels}$   
remember Units

Equation:  $B = \# \text{ bagels}$   
see example 2

you buy?

PROCESS

Step 1 Read and Understand What do you know? You know how much money you have and the price of a bagel and a container of juice.

tells what the variable is

ALWAYS  
Repeat 3 times

What do you want to find out? You want to find out the number of bagel you can buy.

QUESTION  
USE TO DEFINE  
VARIABLES

Step 2 Write key information

Step 3 Define all variables

Step 4 Define equations

SEE NEXT PAGE →

**Example 2** Solve a problem and look back

Solve the problem in Example 1 by carrying out the plan. Then check your answer.

Step 4: Mentally think about a verbal model to help write an equation.

Price of juice (in dollars)	Number of containers	Price of bagel (in dollars)	Number of bagels	Cost (in dollars)
-----------------------------	----------------------	-----------------------------	------------------	-------------------

$$\underline{1.25} + \underline{2} + \underline{.75} \cdot \underline{b} = \underline{7}$$

The equation is:

$$2.50 + .75 B = 7$$

STEP 5: SOLVE

$$\begin{array}{r}
 2.50 + .75 B = 7 \\
 -2.50 \qquad \qquad \qquad -2.50 \\
 \hline
 .75 B = 4.50 \\
 \cdot 75 \qquad \qquad \qquad \cdot 75 \\
 \hline
 B = 6
 \end{array}$$

STEP 6: DOES ANSWER MAKE SENSE

Mentally

Juice	BAGELS	COST
\$1.25 (2)	+\$ .75 (6)	= \$7

$$2.50 + 4.50 = 7$$

Makes Sense 

STEP 7: ANSWER IN A SENTENCE

You can buy 6 bagels.

Your Notes

VOCABULARY:

Formula is an EQUATION THAT RELATES

2 OR MORE QUANTITIES.

BELOW ARE 4 SAMPLE FORMULAS.

FORMULA REVIEW

Temperature

→  $C = \frac{5}{9}(F - 32)$ , where  $F =$  °FAHRENHEIT  
and  $C =$  °CELSIUS

Simple interest

→  $I = Prt$ , where  $I =$  interest,  $P =$  principal  
 $r =$  interest rate (as a decimal), and  $t =$  time

Distance traveled

→  $d = rt$ , where  $d =$  distance,  $r =$  rate,  
and  $t =$  time

MEMORIZE  
THIS ONE!

Profit

→  $P = I - E$ , where  $P =$  profit,  $I =$  income, and  
 $E =$  expenses

How TO DO WORD PROBLEMS:

- ① Write KEY INFO
- ② DEFINE VARIABLE(S)  
\*remember UNITS!
- ③ WRITE EQUATION(S)
- ④ SOLVE (show work clearly)
- ⑤ Check: Ask yourself "DOES THIS ANSWER MAKE SENSE?"
- ⑥ Write answer in a sentence.

KI:

X = (UNIT)

EQ:

} show work  
clearly

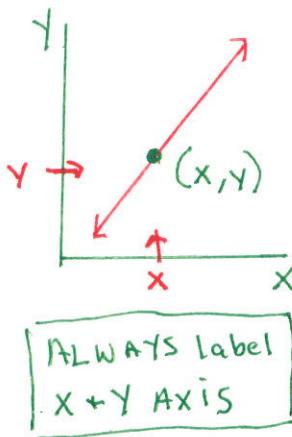
Sentence

## 1.6

## Represent Functions as Rules and Tables

**Goal** • Represent functions as rules and as tables.

Your Notes



**VOCABULARY** RELATION: IS A SET OF ORDERED PAIRS:  $(x, y)$

Function IS A SPECIAL RELATION THAT HAS NO REPEATING X-VALUES. AND Given a graph it passes the Vertical Line Test.

Domain The collection of all x-values.

Range The collection of all y-values.

Independent variable IS THE X VARIABLE

Dependent variable IS THE Y VARIABLE

EXAMPLE:

$(0, 3)$

$(3, 2)$

$(1, 2)$



Adding  $(3, 1)$  would make this NOT a function

X	Y
Domain	Range
INDEPENDENT VARIABLE	DEPENDENT VARIABLE
INPUT	OUTPUT
X	$f(x)$ Means " $y$ "

**Example 1** Identify the domain and range of a function

The input-output table shows temperatures over various increments of time. Identify the domain and range of the function.

x	Input (hours)	0	2	4	6	8
y	Output ( $^{\circ}$ C)	24	27	30	33	33

ADD

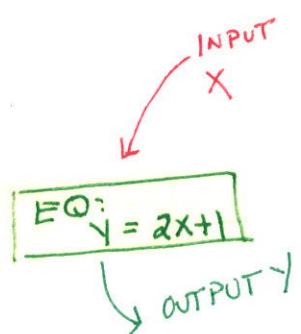
**Solution**

Domain:  $x = 0, 2, 4, 6, 8$

Range:  $y = 24, 27, 30, 33$

ALWAYS PUT NUMBERS LOW TO HIGH

\*do NOT write repeating numbers



### Your Notes

- ✓ **Checkpoint** Identify the domain and range of the function.

Input	4	7	11	13
Output	10	20	35	45

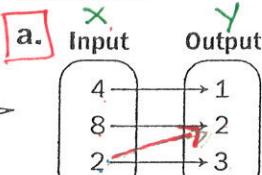
Domain  $x = 4, 7, 11, 13$

Range  $y = 10, 20, 35, 45$

### Example 2 Identify a function

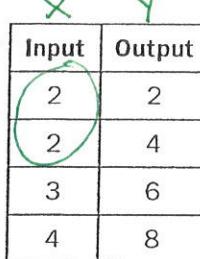
Tell whether the pairing is a function. Explain your reasoning.

#### Solution



↓  
SUGGEST  
Create an  
 $x-y$  Table

x	y
4	1
8	2
2	3
2	2

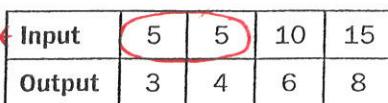
b. 

Input	Output
2	2
2	4
3	6
4	8

NOT A FUNCTION BECAUSE  
THERE ARE REPEATING  
X VALUES (2's)

NOT A FUNCTION  
b/c we have  
repeating  
X values (2's)

- ✓ **Checkpoint** Tell whether the pairing is a function.

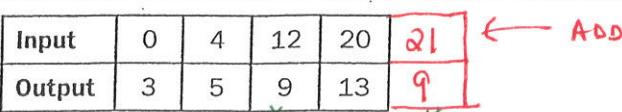
2. 

Input	5	5	10	15
Output	3	4	6	8

NOT A FUNCTION

Circle 5's

b/c there are repeating  
X-values

3. 

Input	0	4	12	20	21
Output	3	5	9	13	9

← ADD

FUNCTION because there are no "x"  
repeating values.

(NOTE, the y-values CAN REPEAT)

### Your Notes

A function may be represented using a rule that relates one variable to another.

$y \leftarrow$   
 $x \leftarrow$

### FUNCTIONS

#### Verbal Rule

The output is 2 less than the input.

#### Equation

$$y = x - 2$$

#### Table

Input $x$	2	4	6	8	10
Output $y$	0	2	4	6	8

### Example 3 Make a table for a function

The domain of the function  $y = 3x$  is 0, 1, 2, and 3. Make a table for the function, then identify the range of the function.

#### Solution

$$\text{EQ } |y = 3x|$$

$x$	0	1	2	3
$y = 3x$	0	3	6	9

← INPUT  
→ OUTPUT

The range of the function is  $y = 0, 3, 6, 9$

### Example 4 Write a function rule

Write a rule for the function.

Input $x$	3	5	7	9	11
Output $y$	6	10	14	18	22

RULE IS AN EQUATION IN THE FORM:

$$y = \underline{\hspace{2cm}}$$

#### Solution

Let  $x$  be the input and let  $y$  be the output. Notice that each output is twice the corresponding input. So, a rule for the function is  $y = 2x$ .

✓ Checkpoint Write a rule for the function. Identify the domain and the range.

4.

Yarn (yd)	1	2	3	4
Total Cost (\$)	1.5	3	4.5	6

Domain:  
 $x = 1, 2, 3, 4$

$$\text{RULE: } |y = 1.5x|$$

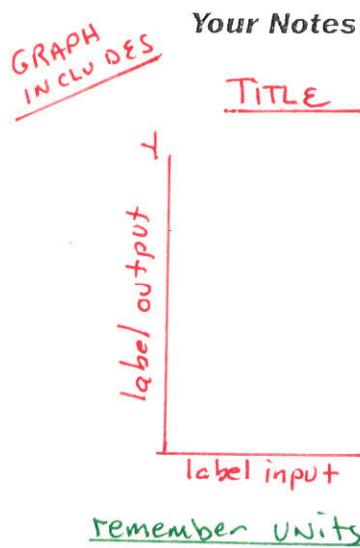
Range:  
 $y = 1.5, 3, 4.5, 6$

$$\text{OR } y = x + \frac{1}{2}x$$



# Represent Functions as Graphs

**Goal** • Represent functions as graphs.



## GRAPHING A FUNCTION

- You can use a graph to represent a FUNCTION.
- In a given table, each corresponding pair of input and output values forms an ORDERED PAIR  $(x, y)$ .
- An ordered pair of numbers can be plotted as a POINT.
- The  $x$ -coordinate is the INPUT. ( $x$ )
- The  $y$ -coordinate is the OUTPUT. ( $y$ )
- The horizontal axis of the graph is labeled with the  $x$ -axis.
- The vertical axis is labeled with the  $y$ -axis.

### Example 1 Graph a function

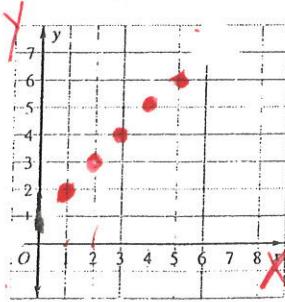
Graph the function  $y = x + 1$  with domain  $1, 2, 3, 4$ , and  $5$ .

#### Solution

Step 1 Make an input-output table.

$x$	1	2	3	4	5
$y$	2	3	4	5	6

Step 2 Plot a point for each ordered pair  $(x, y)$ .

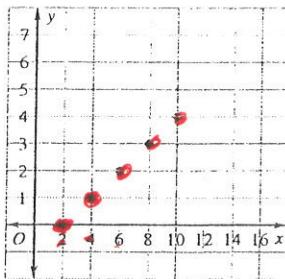


① DO NOT  
DRAW THE LINE!  
(BECAUSE YOU ARE GIVEN  
SPECIFIC DOMAIN  
VALUES)

② LABEL X AND Y.

**Example 2** Write a function rule for a graph

Write a function rule for the function represented by the graph. Identify the domain and the range of the function.

**Solution**

Step 1 Make a TABLE for the graph.

x	2	4	6	8	10
y	0	1	2	3	4

Step 2 Find a Relationship between the input and output values.

Mental work

$$\left\{ \begin{array}{l} \frac{1}{2}(4) = 2 - 1 = 1 \checkmark \\ \frac{1}{2}(6) = 3 - 1 = 2 \checkmark \end{array} \right.$$

Step 3 Write a RULE that describes the relationship.

$y = \frac{1}{2}x - 1$     or     $y = \frac{x}{2} - 1$

A rule for the function is  $y = \frac{1}{2}x - 1$ . The domain of the function is  $x = 2, 4, 6, 8, 10$ .

The range is  $y = 0, 1, 2, 3, 4$

## 1.7 NOTES

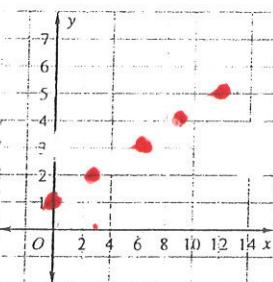
### Your Notes

✓ Checkpoint Complete the following exercise.

1. Graph the function  $y = \frac{1}{3}x + 1$  with domain  $0, 3, 6, 9$ , and  $12$ .

$$y = \frac{1}{3}x + 1$$

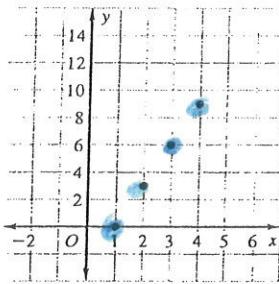
X	0	3	6	9	12
Y	1	2	3	4	5



← Since the domain is stated then **DO NOT DRAW** a line segment

- ✓ Checkpoint Write a rule for the function represented by the graph. Identify the domain and the range of the function.

2.



Homework

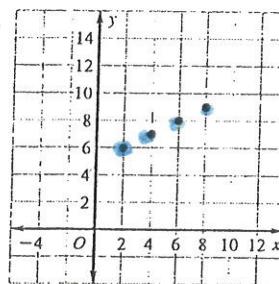
X	1	2	3	4
Y	0	2	4	6

$$D: x = 1, 2, 3, 4$$

$$R: y = 0, 2, 4, 6$$

Rule:  
 $y = 3x - 3$

3.



$$D: x = 2, 4, 6, 8$$

$$R: y = 6, 7, 8, 9$$

Rule  
 $y = \frac{1}{2}x + 5$

$$3(2) - 3 = 3\checkmark$$

$$3(3) - 3 = 6\checkmark$$

$$3(4) - 3 = 9\checkmark$$

$$3(1) - 3 = 0\checkmark$$

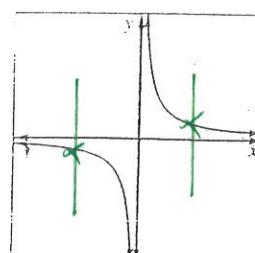
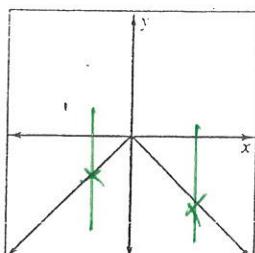
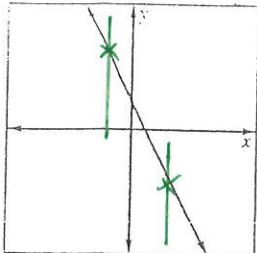
$$y = \frac{1}{2}(2) + 5 = 6\checkmark$$

$$y = \frac{1}{2}(4) + 5 = 7\checkmark$$

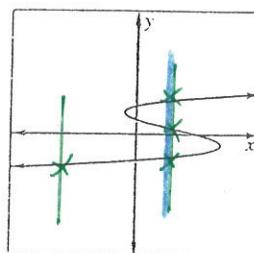
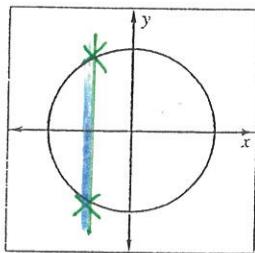
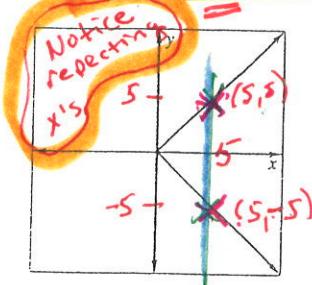
# VERTICAL LINE TEST

## Visual Approach

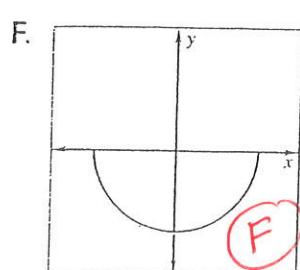
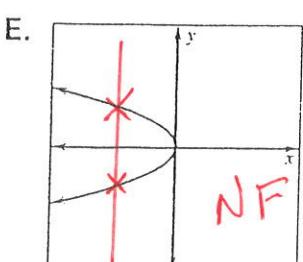
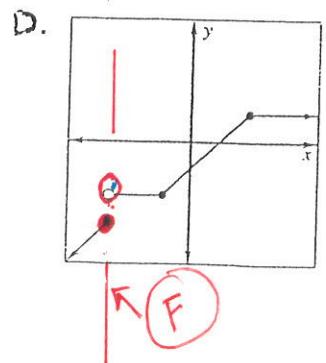
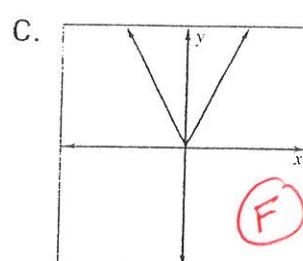
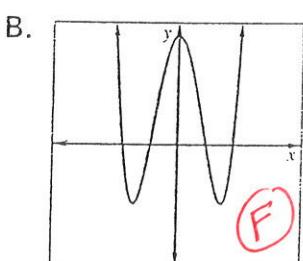
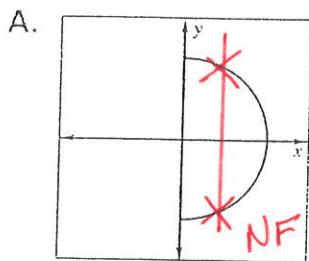
These are **functions**. ↗



These are **not functions**. ↗



Four of the following are functions. Which are they? Circle the letter.



1.7B

YOUR NOTES

What is a function?

FUNCTION IS A  
Special relation  
with NO repeating  
 $X$ -VALUES

What is the  
vertical line test?

ABBREVIATED  
VLINE TEST

To determine if a  
graph is a function,  
use the VLINE TEST.

∴ A VERTICAL LINE  
CAN ONLY TOUCH  
THE GRAPH IN 1  
PLACE TO BE A  
FUNCTION.