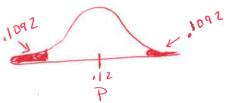


In Exercises 1 to 6, each situation calls for a significance test. State the appropriate null hypothesis H_0 and alternative hypothesis H_a in each case. Be sure to define your parameter each time.

1) Lefties Simon reads a newspaper report claiming that 12% of all adults in the United States are left-handed. He wonders if 12% of the students at his large public high school are left-handed. Simon chooses an SRS of 100 students and records whether each student is right- or left-handed.

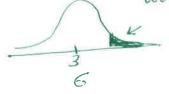
P = proportion of lefties in his school

Ho: P=,12
Ha: P=.12 (the proportion of left.es is NOT 12%)



Cold cabin? During the winter months, the temperatures at the Colorado cabin owned by the Starnes family can stay well below freezing (32°F or 0°C) for weeks at a time. To prevent the pipes from freezing, Mrs. Starnes sets the thermostat at 50°F. The manufacturer claims that the thermostat allows variation in home temperature of $\sigma = 3$ °F. Mrs. Starnes suspects that the manufacturer is overstating how well the thermostat works.

6 = Standard deviation of the temperature in the cabin.



WHEN DEFINING HO + HA ALWAYS!

- 1) Use Population Param eters (PA)
- 2) define population parameter.

competition, the organizers estimate that the variation in distance flown by the athletes will be $\sigma = 10$ meters. An experienced jumper thinks that the organizers are underestimating the variation.

3. Attitudes The Survey of Study Habits and Attitudes (SSHA) is a psychological test that measures students' attitudes toward school and study habits. Scores range from 0 to 200. The mean score for U.S. college students is about 115. A teacher suspects that older students have better attitudes toward school. She gives the SSHA to an SRS of 45 of the over 1000 students at her college who are at least 30 years of age.

M = mean a Hi tude Score on the SSHA for students at least 30 at the college

Ha: M=115 (older students have better attitudes)

- Lefties Refer to Exercise 1. In Simon's SRS, 16 of the students were left-handed. A significance test yields a P-value of 0.2184./2 = 1092
 - (a) Interpret this result in context.
 - (b) Do the data provide convincing evidence against the null hypothesis? Explain.
- (1) IF THE PROPORTION OF LEFTIES AT SIMON'S SCHOOL IS REALLY, 12 THERE IS A 21.84% Chance OF FINDING A SAMPLE OF 100 STUDENTS WITH A VALUE OF P THAT IS AS FAR FROM . 12 AS THE SAMPLE VALUE IN EITHER DIRECTION.
- B THE HIGH P-VALUE (21.84%) DOES NOT PROVIDE CONVINCINC EVIDENCE,

 SOMETHING THAT HAPPENS OVER 20% OF THE TIME JUST BY CHANCE WHEN HO IS TRUE IS NOT STRONG EVIDENCE AGAINST HO (WE WOULD FAIL TO REJECT HO).

In Exercises 7 to 10, explain what's wrong with the stated hypotheses. Then give correct hypotheses.

7. Better parking A change is made that should improve student satisfaction with the parking situation at a local high school. Right now, 37% of students approve of the parking that's provided. The null hypothesis $H_0: p > 0.37$ is tested against the alternative $H_a: p = 0.37$.

THE ALTERNATE HY POTHESIS

GIVES THE CURRENT SITUATION THAN WHAT WE ARE LUOKING FOR EVIDENCE FOR

CORRECTION!

Hn: P=37 Ha: P>,37 [9] Birth weights In planning a study of the birth weights of babies whose mothers did not see a doctor before delivery, a researcher states the hypotheses as

> $H_0: \overline{x} = 1000 \text{ gram's}$ $H_a: \overline{x} < 1000 \text{ grams}$

THE HYPOTHESES ARE ABOUT THE SAMPLE STATISTIC (x) You ALWAYS USE Population paremeters.

CORRECTION. Ho: M = 1000 grams Ha: M < 1000 grams

13 Attitudes In the study of older students' attitudes from Exercise 3, the sample mean SSHA score was 125.7 and the sample standard deviation was 29.8. A significance test yields a P-value of 0.0101.

(a) Interpret the P-value in context.

115 M (b) What conclusion would you make if $\alpha = 0.05$? If $\alpha = 0.01$? Justify your answer.

- If the mean score on the SSHA fur older students at this school is really 115, there is a 1.0170 chance of finding a sample of 45 older students with a mean score of at least 125.7.
- (b) If a = :05 > P-vilue = :0101 THEN REJECT THE NULL HYPOTHESIS HO.

IF d=. OI & p-vilve=, OIOI THEN FAIL TO REJECT THE NULL HYPOTHE SIS

15. Is this what P means? When asked to explain the meaning of the P-value in Exercise 13, a student says, "This means there is only probability 0.01 that the null hypothesis is true." Explain clearly why the student's explanation is wrong.

2

125.7

EITHER HO IS TRUE (PROBABILITY THAT HO IS TRUE IS 1) OR HO IS FALSE (PROBABILITY THAT Ho is TRUE is 0) A P-VALUE of 0.01 means that if Ho is true, then the chance of the volve we obtained or with avoive that is more extreme is 120,

refer to the following setting. Slow

HO TRUE

HO FALSE

TYPE CORRECT CORRECT

SECTION

response times by paramedics, firefighters, and policemen can have serious consequences for accident victims. In

the case of life-threatening injuries, victims generally need

cities have begun to monitor emergency response times.

In one such city, the mean response time to all accidents involving life-threatening injuries last year was $\mu = 6.7$

minutes. Emergency personnel arrived within 8 minutes

after 78% of all calls involving life-threatening injuries last year. The city manager shares this information and encour-

ages these first responders to "do better." At the end of the year, the city manager selects an SRS of 400 calls involving

life-threatening injuries and examines the response times.

determine whether the average response time has

decreased. Be sure to define the parameter of interest. (b) Describe a Type I error and a Type II error in this setting, and explain the consequences of each. (c). Which is more serious in this setting: a Type I

(a) State hypotheses for a significance test to

medical attention within 8 minutes of the accident. Several

Exercises 19

19. Awful accidents

Exercises

M= mean response time for all accidents involving life threatening INJORIES IN THE

Ho. 11 = 6.7 min HA: M < 6.7 Want to do better M

6.7

193

TYPE I ERRUR: false positive & The city Concil concludes the response time his improved

when it has Not. TYPEI ERRUR false negative B The city council Concludes that the response time has not improved when it

really has TYPE I DERRUR WOUld be wurse. The city may stop trying to

improve its response fines the because they think they have met the goal when in fact they have not, MORE PEUPLE QUILD DIE.

Opening a restaurant You are thinking about opening a restaurant and are searching for a good location. From research you have done, you know that the mean income of those living near the restaurant must be over \$85,000 to support the type of upscale restaurant you wish to open. You decide to take a simple random sample of 50 people living near one potential location. Based on the mean income

error or a Type II error? Justify your answer.

restaurant there.8 (a) State appropriate null and alternative hypotheses. Be sure to define your parameter.

of this sample, you will decide whether to open a

(b) Describe a Type I and a Type II error, and explain the consequences of each.

(c) If you had to choose one of the "standard" significance levels for your significance test, would you choose $\alpha = 0.01, 0.05$, or 0.10? Justify your choice.

M= THE MEAN INCOME OF RESIDENTS NEAR THE RESTAURANT.

Ho! M= \$85,000

HA! U >\$ 85,000



RESTAURANT IN (b) TYPE I EREUR : OPEN THE ALOCATION WHERE THE RESIDENTS WILL NOT BE ABLE TO SUPPORT IT.

TYPE IL ERRUR: DO NOT OPEN A RESTAURANT IN ALOCATION WHERE THE RESIDENTS IN FACT SUPPORT IT FINANCIALLY.

A TYPE I ERROR WOULD BE WORSE IN SELECTING A LOCATION TO OPEN THE RESTAURANT. SO IT WOULD BE BETTER TO CHOSE &=,01 TO MINIMIZE THE RISK OF A TYPE I ERRUR

23 Error probabilities You read that a statistical test at significance level $\alpha = 0.05$ has power 0.78. What are the probabilities of Type I and Type II errors for this test?

a=.05 POWER = . 78 POWER = 1-B · 78=1-B

P(TYPEI ERRUE) = 2 = ,05 P (TYPE II ERROR) = B = ,22 (1-.78) M= the mean nicotine content of their cigarettes.

A certain cigarette brand advertises that the mean nicotine content of their cigarettes is 1.5 mg, but you are suspicious and plan to investigate the advertised claim by testing the hypotheses $H_0: \mu = 1.5$ versus $H_a: \mu > 1.5$ at the $\alpha = 0.05$ significance level. You will do so by measuring the nicotine content of 30 randomly selected cigarettes of this brand.

HA: 11715

(a) Describe what a Type I error would be in this context. Felse positive (a)

Conclude that the mean nicotine content per cigorette is greater than 1.5 mg when it is Equal to (OR LESS THAN)

(b) Describe what a Type II error would be in this context. felse here (B) Not Conclude that the mean nico time level is greater than 1.5 mg per Cigarette when it is

(c) From the perspective of public health, which error—Type I or Type II—is more serious? Explain.

A TYPE II ERROR WOOLD MEAN THAT YOU FAIL TO DISCOUR THAT THE CIGARETTES HAVE A HIGHER NICOTINE CONTENT THAT THE COMPANY CLAIMS, WHICH MEANS PEOPLE WILL BE EXPUSED TO MORE NICOTINE THAT THEY EXPECT AND THIS WOULD BE A PUBLIC HEALTH ISSUE! A TYPE I ERROR MICHT BRING UNWARRANTED NEGATIVE PUBLICITY TO THE TOBALLO COMPANY BUT NOT A HEALTH

(d) Explain why it might be a good idea to increase the significance level to 0.10 for this test. YOU WANT TO MINIMIZE THE CHANCE OF MAKING A TYPE II ERROR (NOT FINDING THAT THE NICOTINE LEVEL IS HIGHER THAN HIGHER SIGNIFICANCE LEVEL (2) WHICH WILL IN CREASE THE

POWER OF THE TEST,

(e) You have determined that at the $\alpha = 0.05$ significance level, the power of the test against the alternative $\mu = 1.75$ is 0.88. Explain what the power of the test means in the context of the problem. POWER = . 88 measures the probability of

rejecting the null hypothesis and concluding that the true mean hico time level is above 1.5 when IT is in Fact 1.75 mg

(f) What impact will reducing the significance level to 0.01 have on the power of the test?

1175 Reducing & from , 05 to , 01 (the significance level) Shift do will increase the probability of a Type II error, so it reduces the power. You can see this relationship by shifting the red line to the right

12. "Red tide" is a bloom of poison-producing algae—a few different species of a class of plankton called dinoflagellates. When weather and water condition cause these blooms, shellfish such as clams living in the area develop dangerous levels of a paralysis-inducing toxin. In Massachusetts, the Division of Marine Fisheries (DMF) monitors levels of the toxin in shellfish by regular sampling of shellfish along the coastline. If the mean level of toxin in clams exceeds 800µg (micrograms) of toxin per kg of clam meat in any area at a 5% level of significance, clam harvesting is banned there until the bloom is over and levels of toxin in clams subside. During a bloom, the distribution of toxin levels in clams on a single mudflat

9.100mz

(a) Define the parameter of interest and state appropriate hypotheses for the DMF to test.

is distinctly non-Normal.

(b) Because of budget constraints and the large number of coastal areas that must be tested, the DMF would like to sample no more than 10 clams from any single area. Explain why this sample size may lead to problems in carrying out the significance test from (a).

(c) Describe a Type I and a Type II error in this situation and the consequences of each.

TYPEI ERROR: Concluding that the mean revel of toxin is above
800 uglky When it is normal. Consequence: The DMF
woold close the area to clam howesting which would
have a negative economic impact on anyone who depends
on the clam business, even though the clams are safe to eat. TYPE I ERROR: NOT CONCLUDING THAT THE MEAN LEVEL OF TOXINS IS ABOVE SAFE LEUELS WHEN IT IS, CONSEQUENCE! THIS COULD CAUSE ANYONE WHO EATS CLAMS FROM THIS AREA TO BECOME SICK OR EVEN DIE.

(d) The DMF is considering changing the significance level of the test to 10%. Discuss the impact this might have on error probabilities and the power of the test, and describe the practical consequences of this change.

RAISING THE SIGNIFICANCE LEVEL TO 1000 WOULD INCREASE THE PROBABILITY OF A TYPE I ERRUR BUT DECREASE
THE PROBABILITY OF A TYPE II ERRUR AND INCREASE THE POWER OF THE TEST. THIS WOULD DECREASE THE LIKELI HOOD OF PEOPLE ENTING TOXIC CLAMS, SO IT MICHT BE A GOOD IDEA. BETTER SAFE THAN SURRY.